

**Managing drought and scarcity in semi-arid lands:
The cases of California and Spain**
17 January 2015

**Botín Foundation / Rosenberg International Forum on Water Policy
Madrid, January 29, 2015**

Session 4: Responding to drought

The role of groundwater in Spain in coping with scarcity

Contents

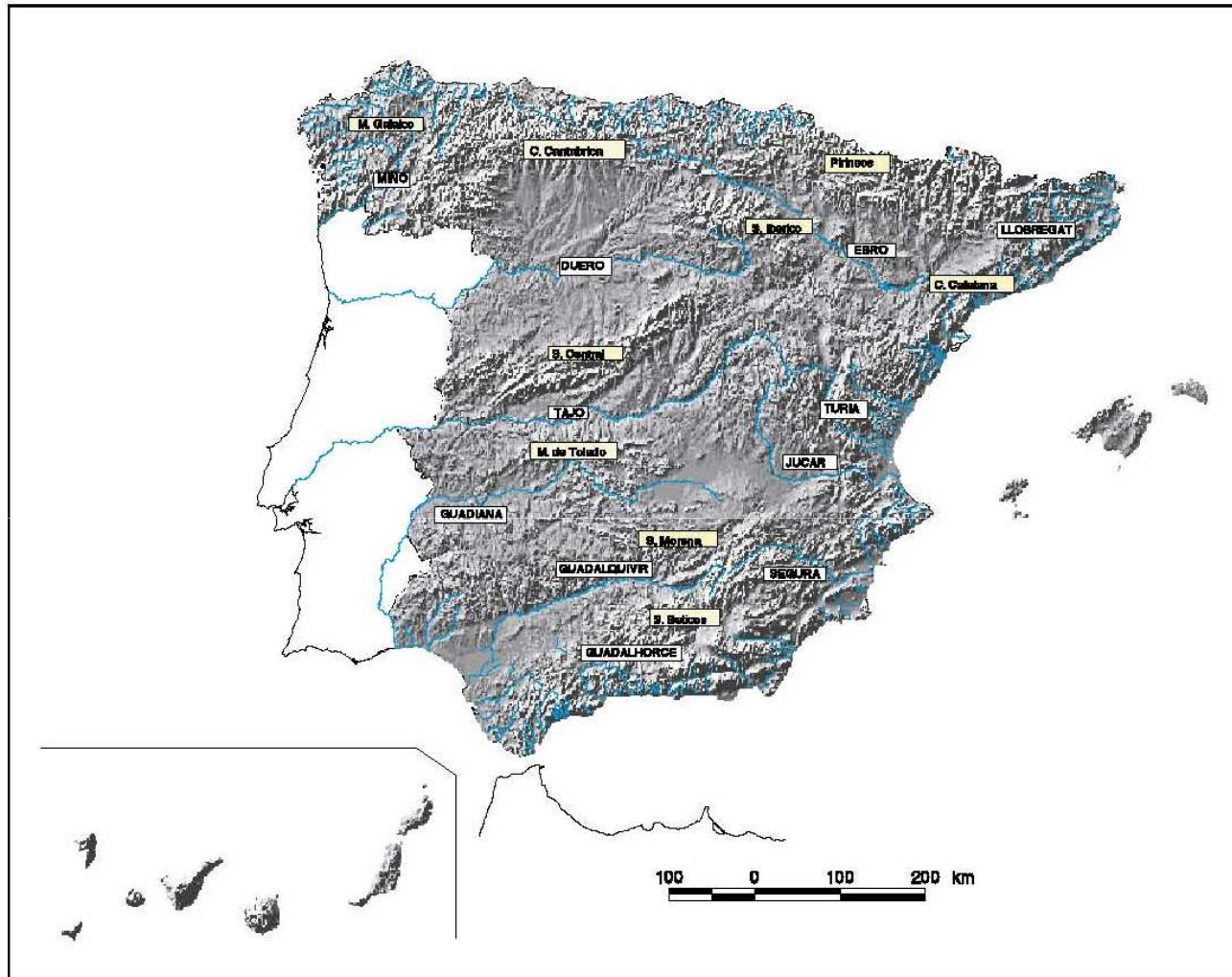
Aquifers and aquifer recharge in Spain
Legal and administrative conditions
Water and groundwater scarcity
Intensive groundwater use and mining: the MASE project
Groundwater quality and environmental aspects
Social and economic issues
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Surface and groundwater joint and alternative use

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Water Observatory, Botin Foundation**

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River basins in Spain and relief



About 1000 km to the SW,
in front of the Sahara coast

Territories:

The Iberian Peninsula

The archipelagos { Balearic Is.
Canary Is.

About 500,000 km²

**Mountaineous
Small plains**

2/3 to the Atlantic Ocean
1/3 to the Mediterranean Sea

Rivers:

- effluent and influent
- effemeral in some tracts
- high slope

Water administration

- river basins
- islands

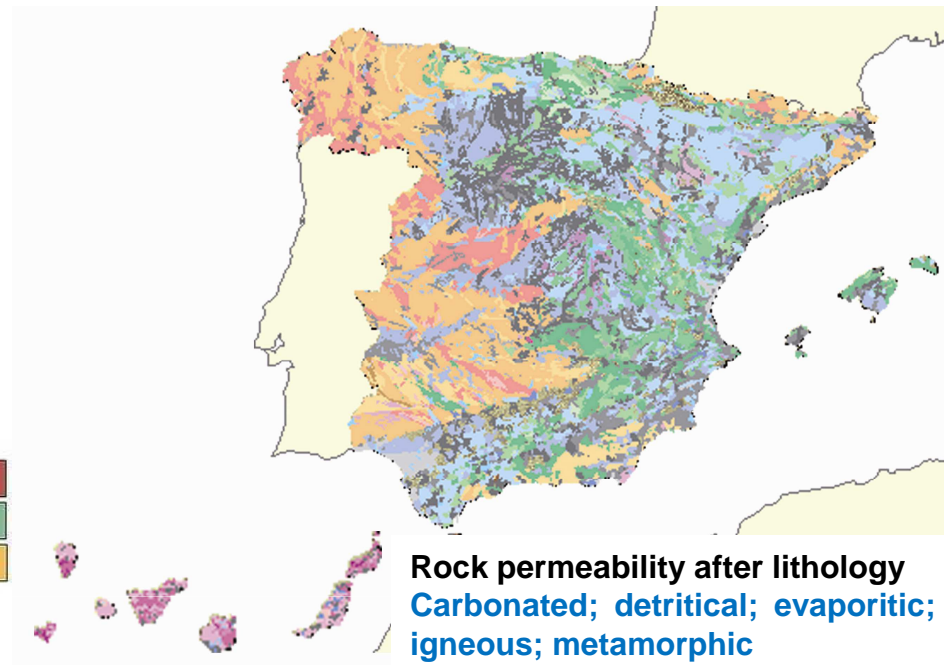
Irrigation
Population
Tourism
Industry

**Mostly in:
Center
Med. Area**

Aquifers in Spain. Main lithologies



Main dominant rock types
Siliceous; carbonated; clayish/detrital



Litología: Permeabilidad de la litología

(-)	DETRÍTICAS - MUY ALTA	VOLCÁNICAS (PIROCLÁSTICAS Y LÁVICAS) - BAJA	DETRÍTICAS (CUATERNARIO) - MUY ALTA
CARBONATADAS - MUY BAJA	DETRÍTICAS - ALTA	VOLCÁNICAS (PIROCLÁSTICAS Y LÁVICAS) - MUY BAJA	DETRÍTICAS (CUATERNARIO) - ALTA
CARBONATADAS - BAJA	DETRÍTICAS - MEDIA	ÍGNEAS - BAJA	DETRÍTICAS (CUATERNARIO) - MEDIA
CARBONATADAS - MEDIA	EVAPORÍTICAS - MEDIA	ÍGNEAS - MUY BAJA	DETRÍTICAS (CUATERNARIO) - BAJA
CARBONATADAS - ALTA	EVAPORÍTICAS - BAJA	METADETRÍTICAS - BAJA	Sin datos
CARBONATADAS - MUY ALTA	EVAPORÍTICAS - MUY BAJA	METADETRÍTICAS - MUY BAJA	
Masa de agua superficial	VOLCÁNICAS (PIROCLÁSTICAS Y LÁVICAS) - ALTA	METADETRÍTICAS - ALTA	
DETRÍTICAS - MUY BAJA	VOLCÁNICAS (PIROCLÁSTICAS Y LÁVICAS) - MUY ALTA	METADETRÍTICAS - MEDIA	
DETRÍTICAS - BAJA	VOLCÁNICAS (PIROCLÁSTICAS Y LÁVICAS) - MEDIA	DETRÍTICAS (CUATERNARIO) - MUY BAJA	

Intensive geologic disturbance

Few large aquifers

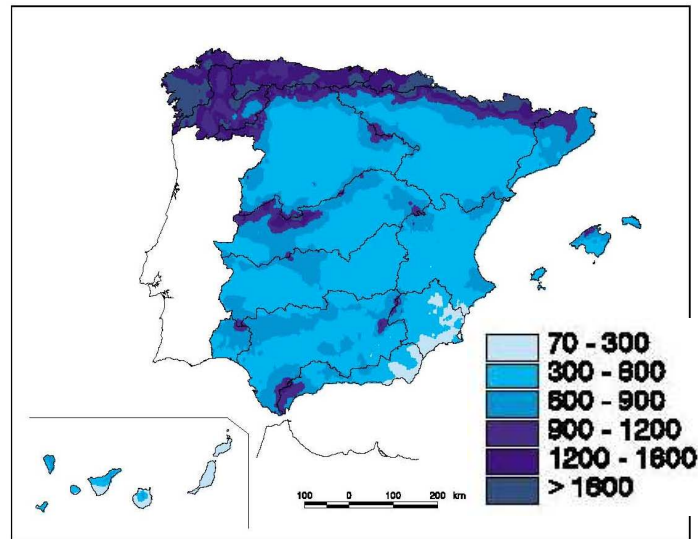
Small, moderate size, unconsolidated aquifers (100–600 km²)

Small-size thick, highly productive, low storage carbonate aquifers, in the E and S

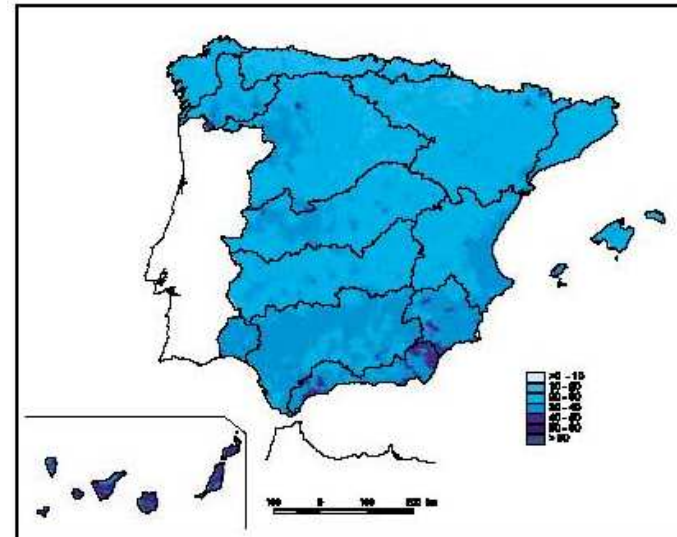
Volcanic aquifers in the Canaries

→ 50.000 km² in the Central Valley of California

Rainfall and groundwater recharge in Spain

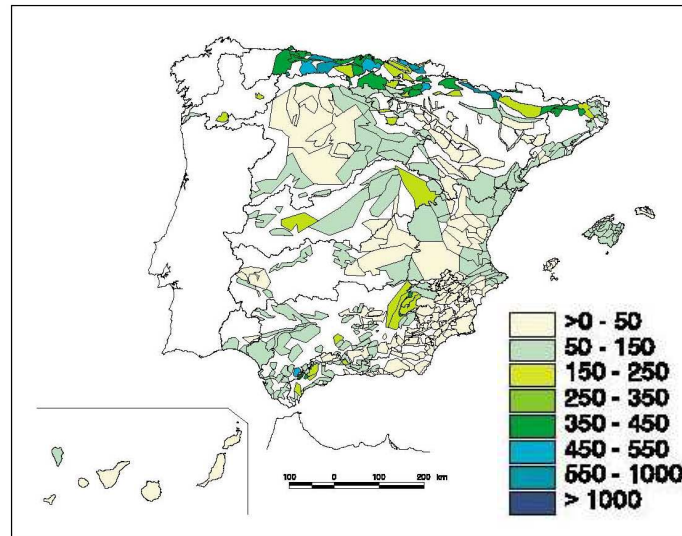


Average rainfall in mm/yr
LBA 2000

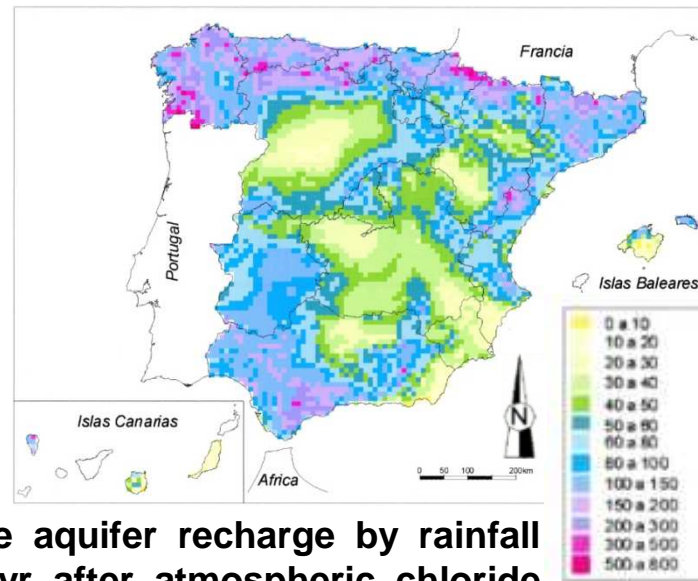


Coefficient of variation of yearly rainfall (%)
LBA 2000

Semi-arid
conditions:
Centre
Mediterranean
side



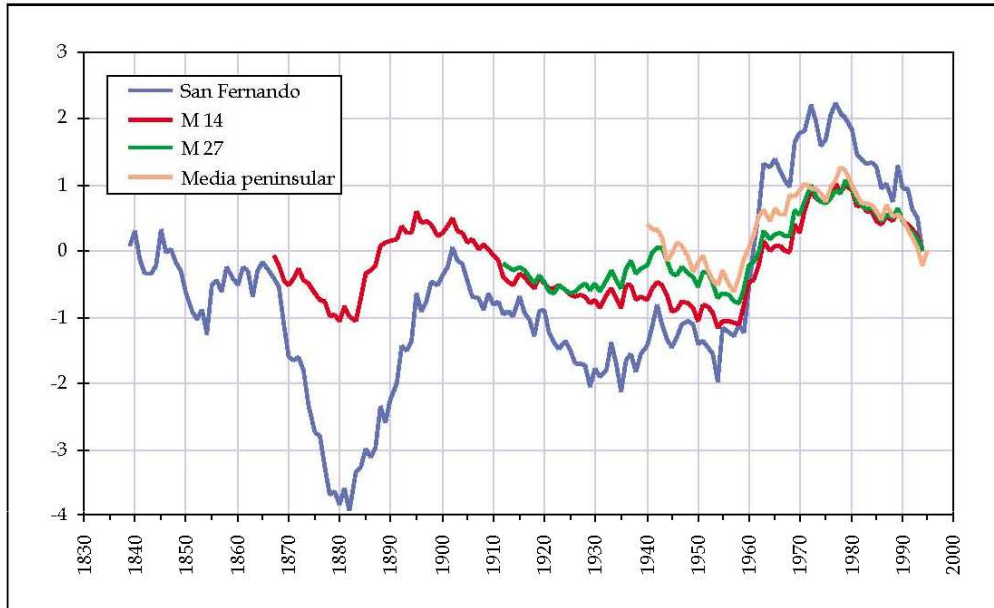
Average aquifer recharge by rainfall
in mm/yr
LBA 2000



Average aquifer recharge by rainfall
in mm/yr after atmospheric chloride
deposition balance
(Alcalá and Custodio, 2010)

Arid
conditions:
part of the
Canary
Islands

Rainfall and water resources variability

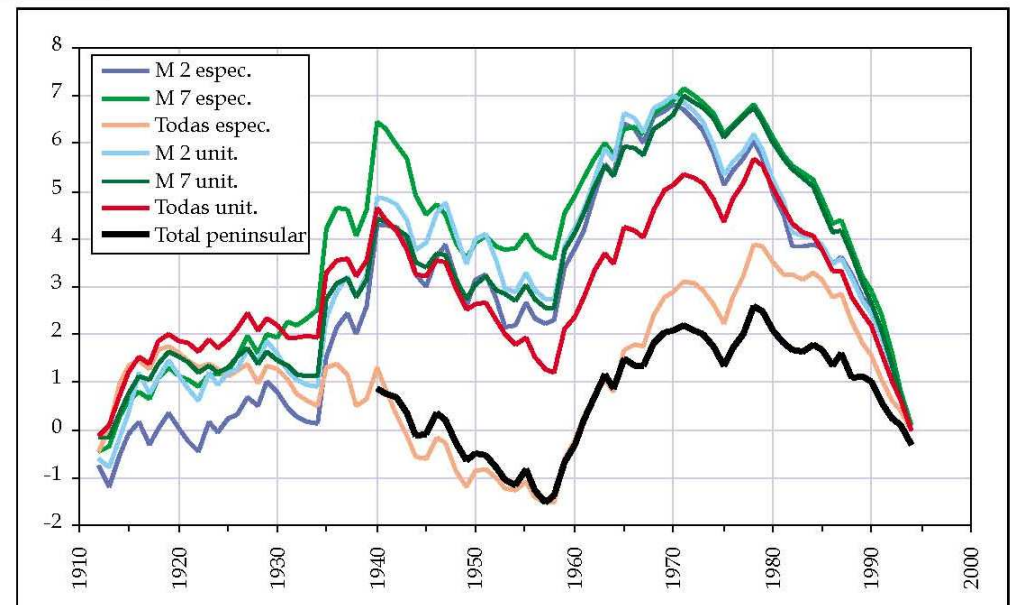


Cumulative deviation from the mean of the period
 Values in metres

Annual water resources.
 Period 1910–1995

Annual precipitation. Various total periods.
 The longest period 1840–1995

High irregularity
 Cyclic behaviour of 10 and 20 years
 3–5 years
 Long dry/wet periods

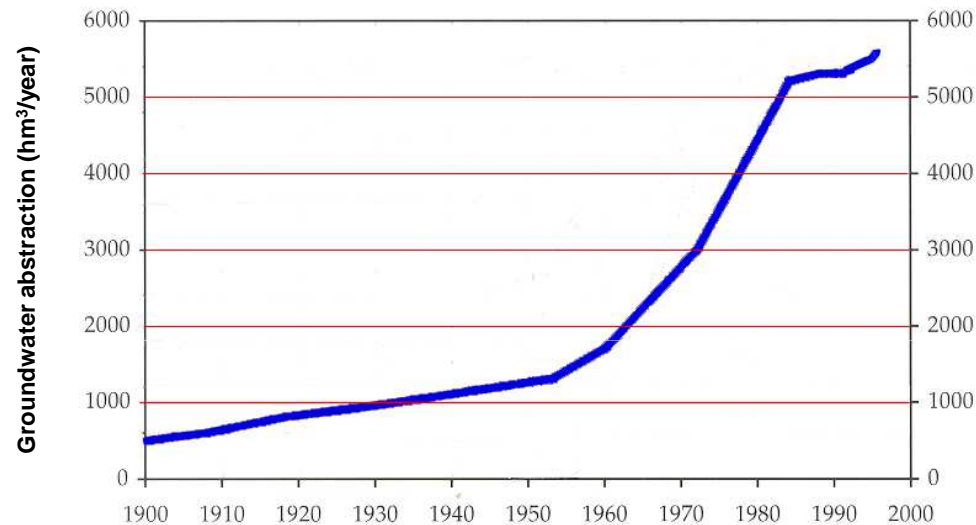


LBA, 2000

Some approximate definitions applied to groundwater

- Reserves:** aquifer volume x drainable porosity
- Intensive development:** a significant fraction of recharge is abstracted
 important changes in the aquifer flow system
 in its relation with other water bodies
 drawdown may be large and increasing along time
- Overexploitation:** Negative effects observed on groundwater quantity and quality
 Subjective
 Hydrodynamic effects not considered
 A legal term in Spain
 Its use should be discouraged
- Renewable resources:** ~ total net recharge
 Variable according to circumstances: specify them
- Exploitable resources:** Those that can be abstracted with bearable consequences
 Depends on **what is bearable**
 economically, environmental, socially and politically
This is not a true technical result but a social and political decision
- Groundwater mining** \equiv sustained use of groundwater reserves
 It implies: abstraction > recharge \rightarrow steady state not possible
 It is a long-term evaluation
 When recovery needs > 50 years after abstraction ceases
 When freshwater storage is changed into saline water

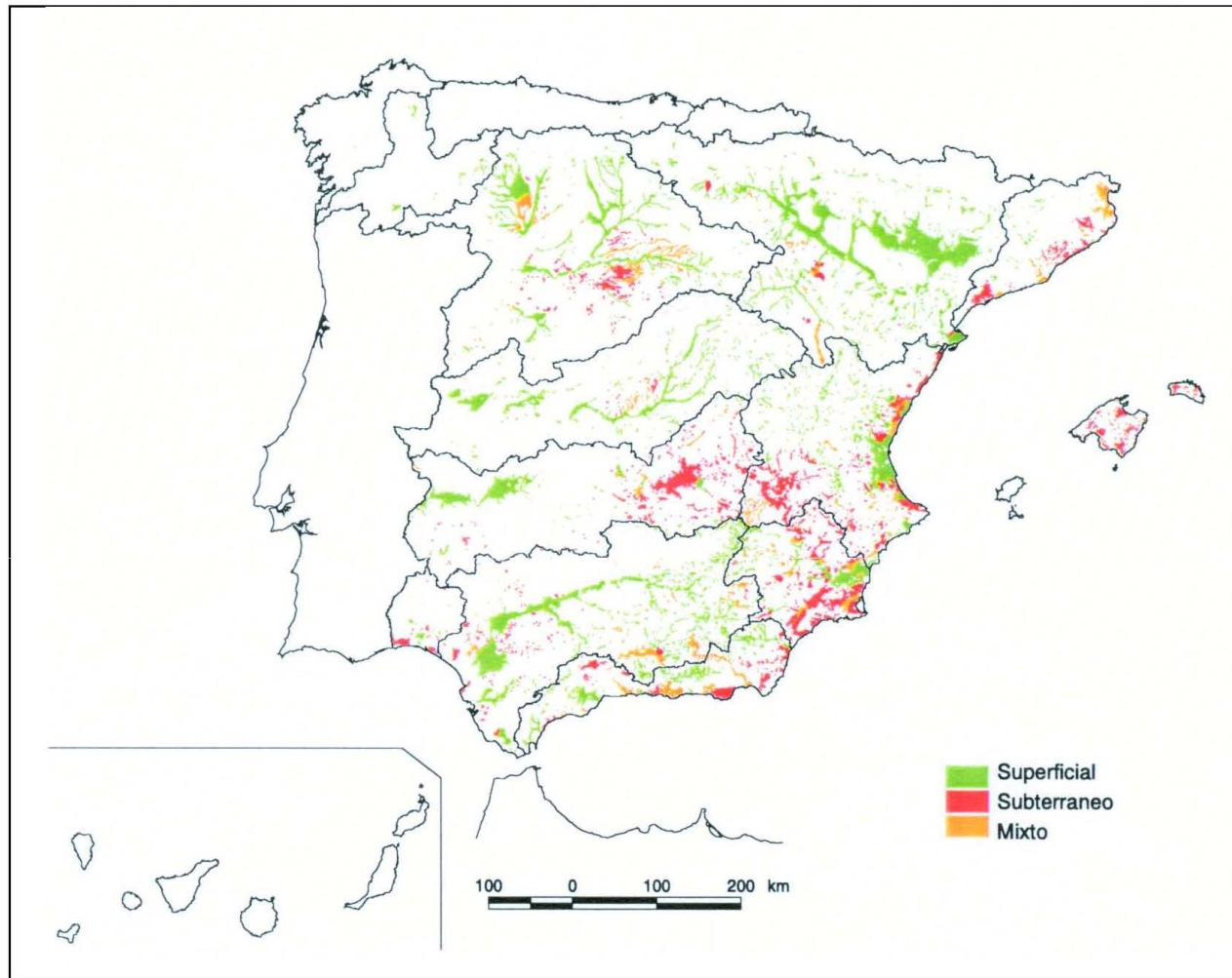
Groundwater development in Spain



Groundwater abstraction in Spain in hm³/year

Current value is 7 km³/year
Start of intensive groundwater development in the 1950s
Trend to stabilization after the 1980s

Groundwater use in agriculture in Spain



Map of irrigated zones with indication of water origin LBA, 2000

**Agriculture uses 80% of GW resources in the Peninsula
50–60% in the archipelagos:
Mallorca, Gran Canaria, Tenerife, La Palma and Gomera**

Legal conditions of groundwater in Spain

Water Act 1866 → all water in the public domain

1879 → groundwater in the private domain

1985 → **all water is a public domain**

→ to avoid expropriation of existing groundwater rights: **legal options**

- right holders • get public protection (?) by giving their rights
 maintain the rights for 50 years
 preference for a concession
 go to a registry

- preserve their rights forever
 without changing well characteristics (??)
 go to a catalogue

- reality → **few owners have changed** their status
 pre-law development was already intensive

→ **most groundwater is private in practice**

→ the inventory of groundwater rights is very incomplete

→ **overexploitation areas** can be declared by water authorities

owners in overexploited areas have to $\left\{ \begin{array}{l} \text{adapt their abstraction} \\ \text{form an users' association} \end{array} \right.$

→ **mostly a failure**

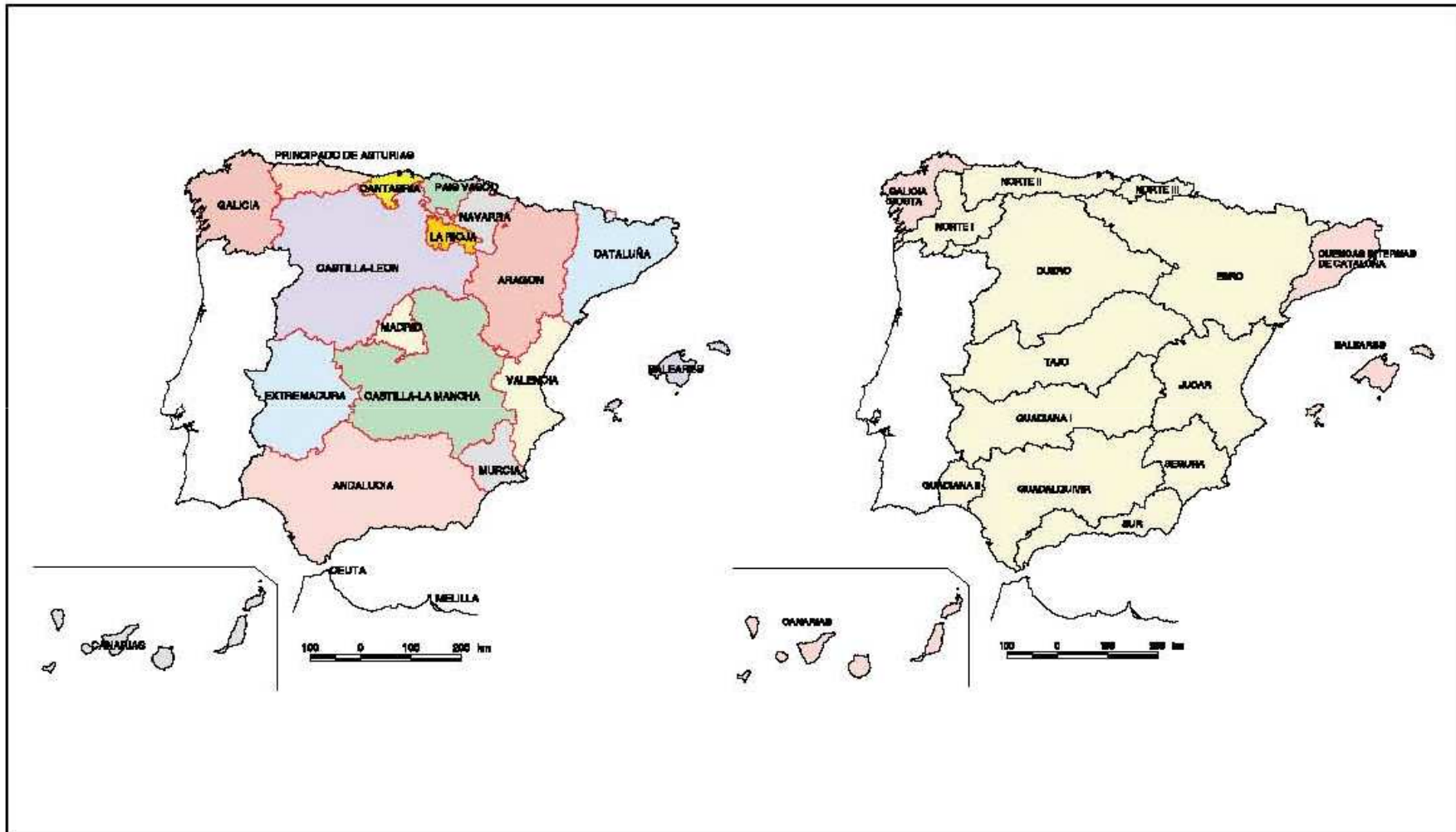
→ **groundwater users associations** → public entities → some **existing**

2001 → incorporation of the European Water Framework Directive of year 2000

→ successive modifications → European “Groundwater Directive” of year 2006

→ the main problems are not properly addressed

Administrative framework of groundwater in Spain



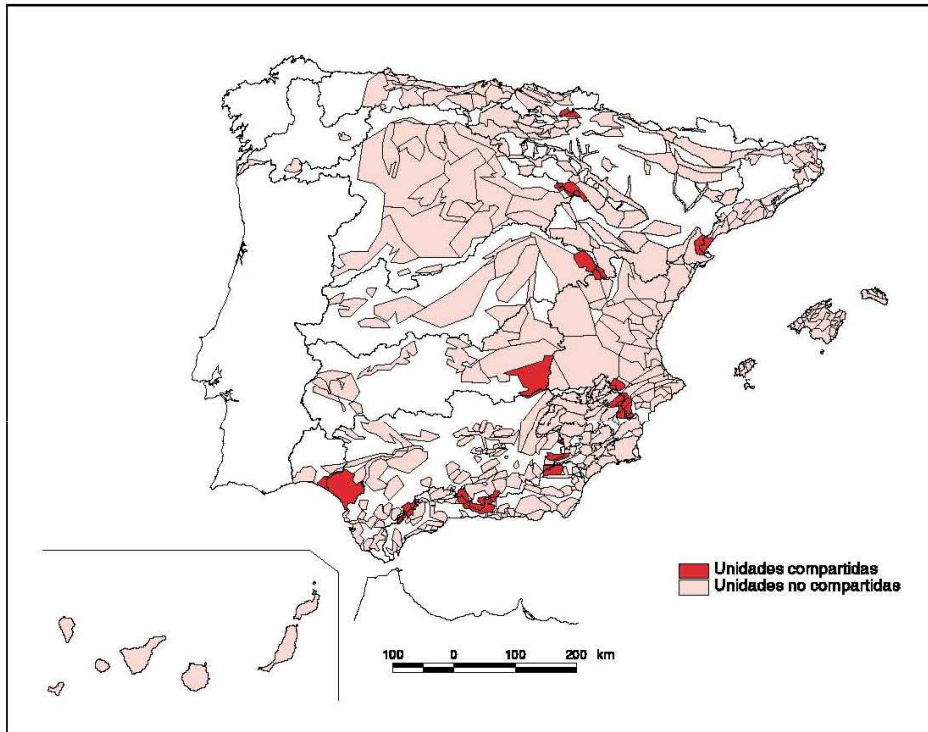
Political division in Autonomous Regions

Responsible of water resources and the environment
but not of water management in shared basins

Administrative framework of water and groundwater in Spain

Often Regions and River Basins do not coincide

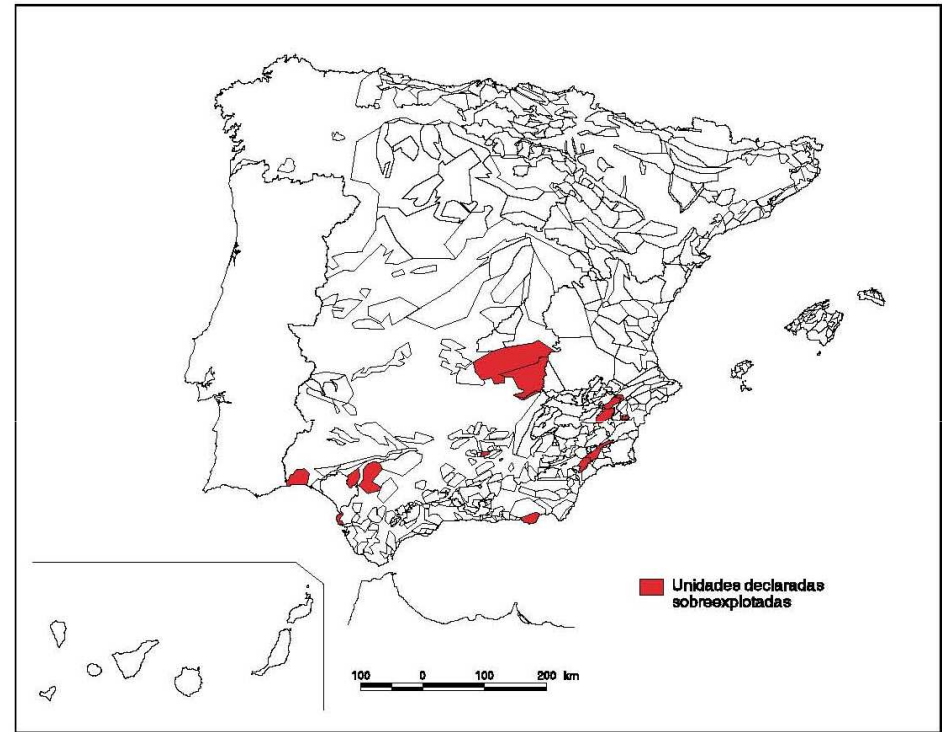
Map of hydrogeological units with shared units between water administrations



In pink → non-shared units
 In red → shared units
 LBA, 2000

Some shared units are intensively exploited
 → difficult management

Map of hydrogeological units with a some declaration of “overexploitation” in 1996



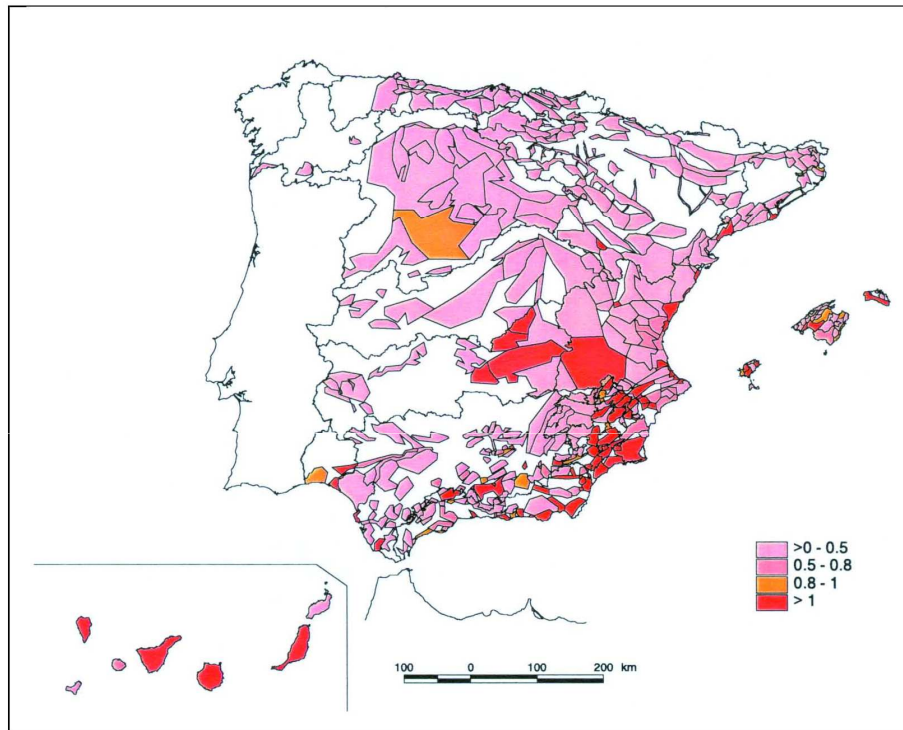
In red : official «overexploited units»
 LBA, 2000

There are many more
 After 25 years only a few have completed the procedure

Groundwater scarcity

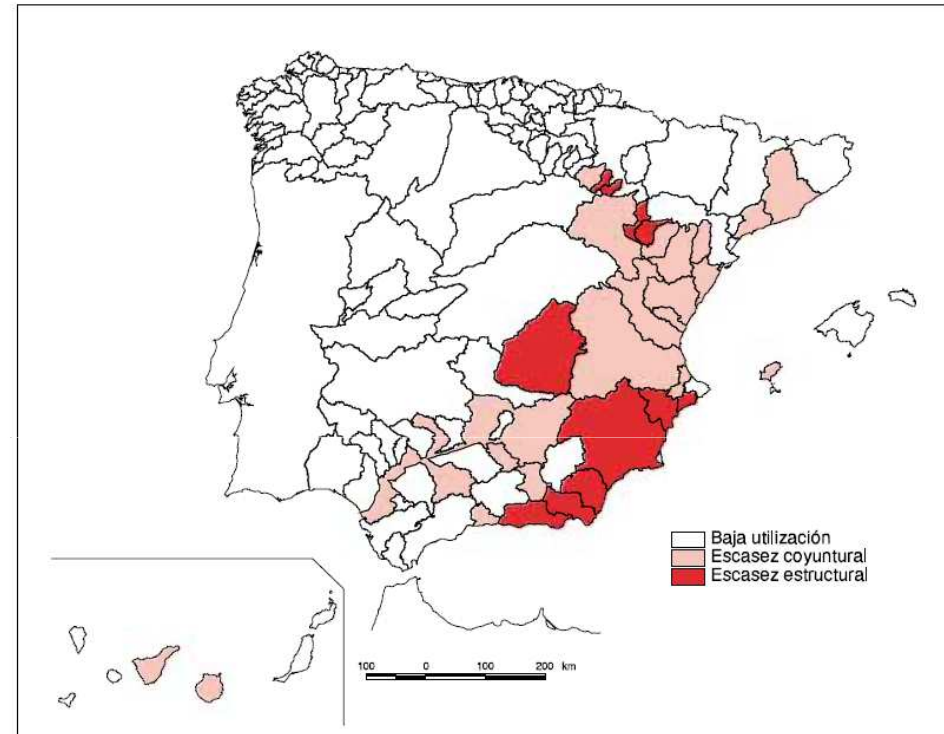
Ratio of groundwater abstraction to recharge by hydrogeological units

Excess of groundwater exploitation in hydrogeological units



LBA, 2000

Great intensity of groundwater exploitation
in { the South-east
the Canaries
Recharge is exceeded in some areas



LBA, 2000

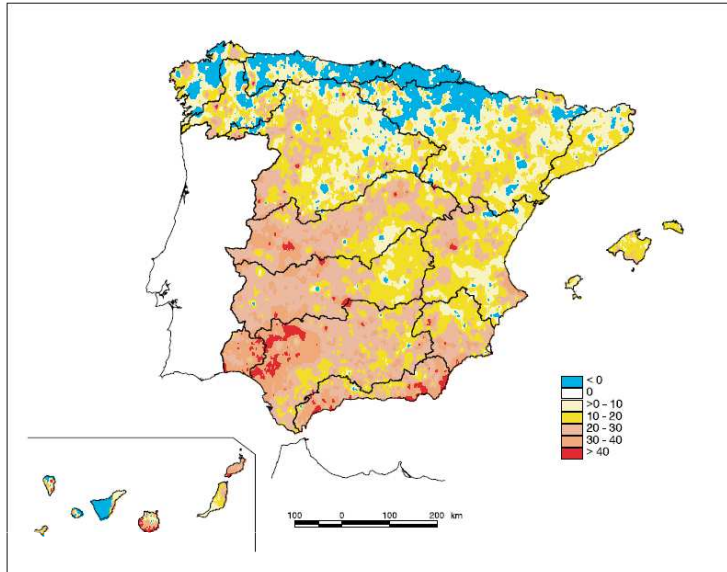
Legend: low use
occasional scarcity
«structural» scarcity

Total GW values in km ³ /year		
	Península	Islands
Recharge	31	1,2
GW abstraction	7	0,6

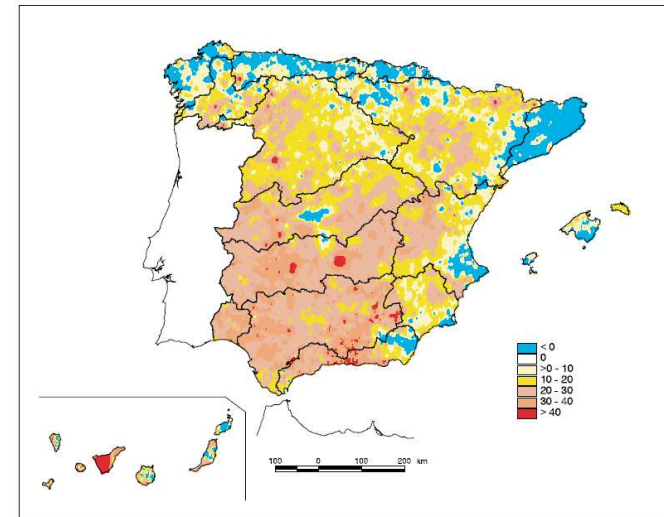
LBA, 2000

Changes in water resources in drought periods

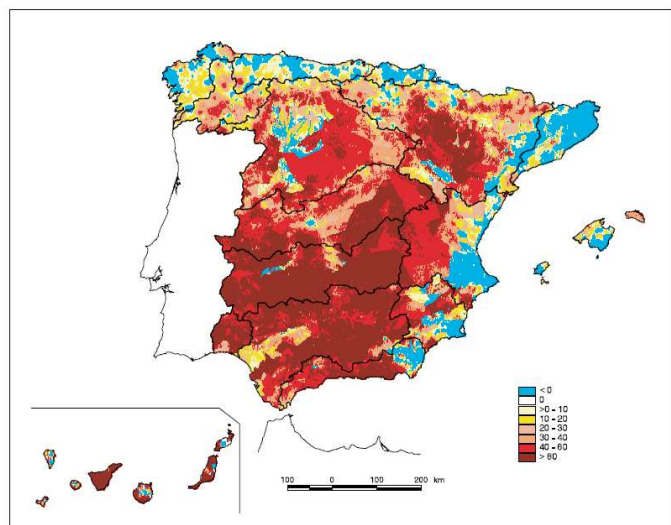
Percent reduction relative to the 1940–41/1995–96 period



Average rainfall decrease
1979–80/1982–83 period



Average rainfall decrease
1990–91/1994–95 period



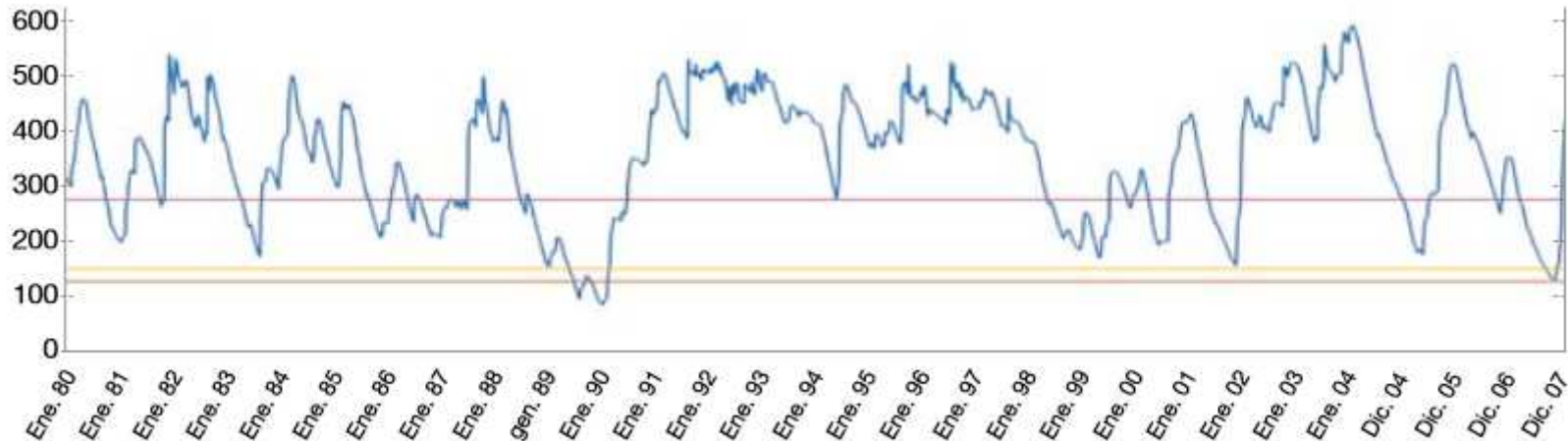
Average water resources
decrease
1990–91/1994–95 period

Changes } not coincident in the territory
Severity }

Surface water systems suffer the more
→ even in wet areas

Groundwater systems are resilient

Current groundwater use in Spain in droughts



Water volume stored in the Ter-Llobregat system for the water supply of **Barcelona**

Thresholds for situations of: emergency; exceptionality; high exceptionality

They are often attained

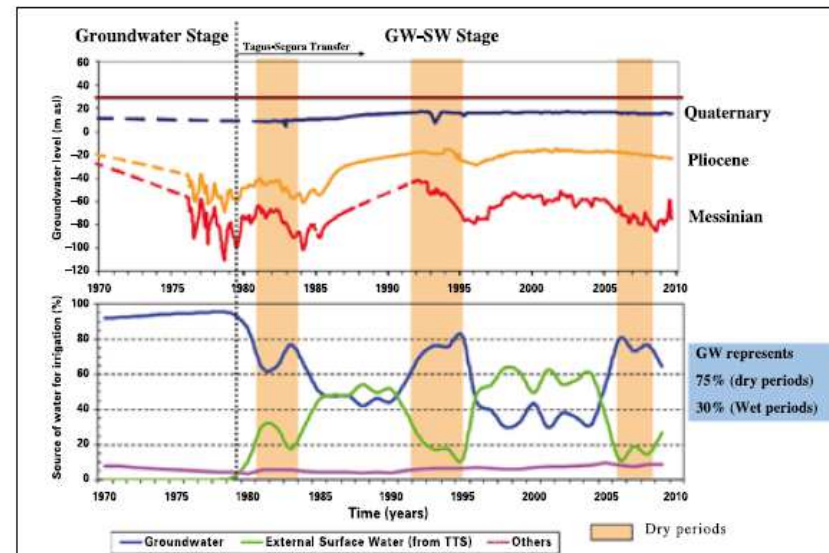
Solutions: lower Llobregat aquifer **storage** depletion + others

Campo de Cartagena area (Murcia)

Groundwater is intensively used in droughts

when { imported/industrially produced water fails/is scarce/is too expensive

In the Mediterranean area “drought wells” are used for town and agriculture supply during droughts



The MASE project

MASE = Minería del agua subterránea en España
Groundwater mining in Spain

Executed: Department of Geo-Engineering, Technical University of Catalonia (UPC)

Prepared by : E. Custodio

Financial support: AQUALOGY

Supervision: CETaqua

Considered aspects {

- hydrology / hydrogeology
- environment
- economics
- social issues
- administrative issues
- ethic issues

Use of data in {

- in existing reports and studies (non-exhaustive)
- from information from experts {
 - contributions
 - questionnaire

No specific studies.

Areas considered: **South-eastern Spain** (Levante): southern Alacant, Murcia and Almeria
The Canary Islands: Gran Canaria, Tenerife

The MASE project

Results

evaluation of groundwater intensive use and its consequences

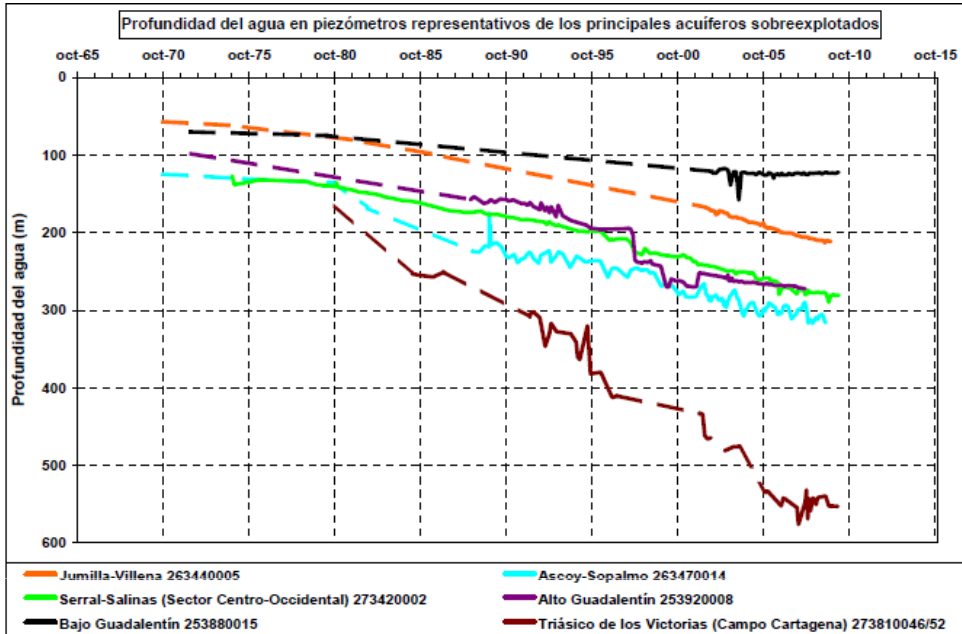
importance for development and prospective

estimated groundwater mining:

- 15 km³** in south–eastern Spain
- 0.3–0.5 km³** in Gran Canaria Island
- 2 km³** in Tenerife Island

partial volume recovery is possible after ceasing abstraction

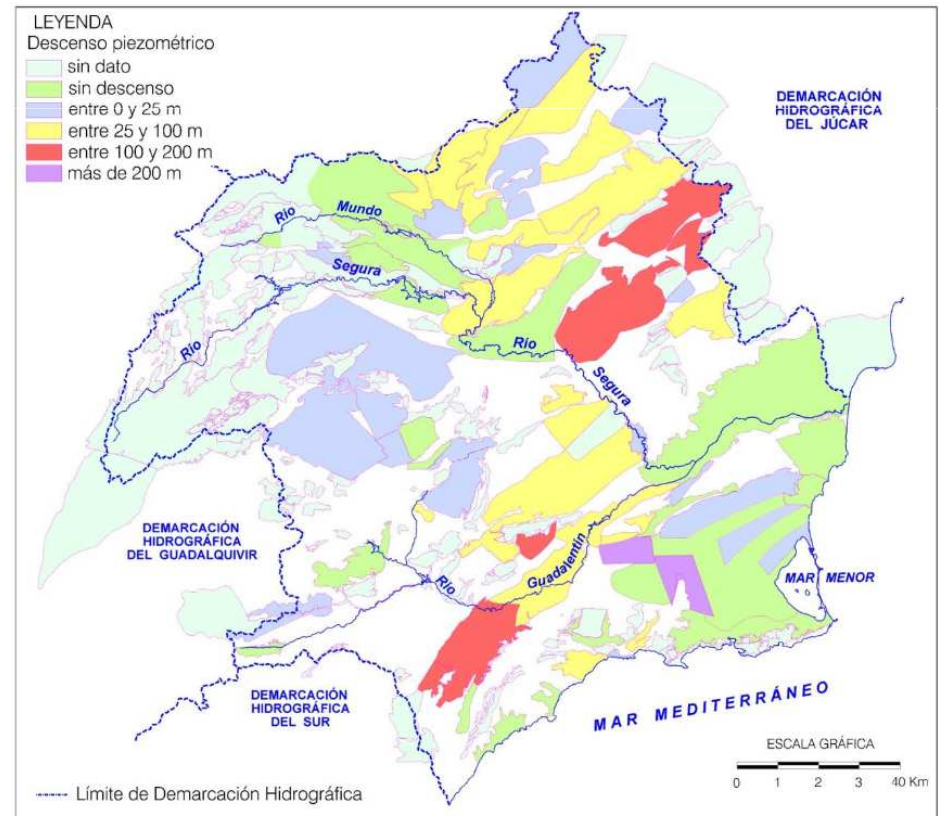
- there is some significant recharge
- from some decades to some centuries (?)
- in Tenerife a part of the mid–to–top island is permanently drained by water galleries (long water tunnels)

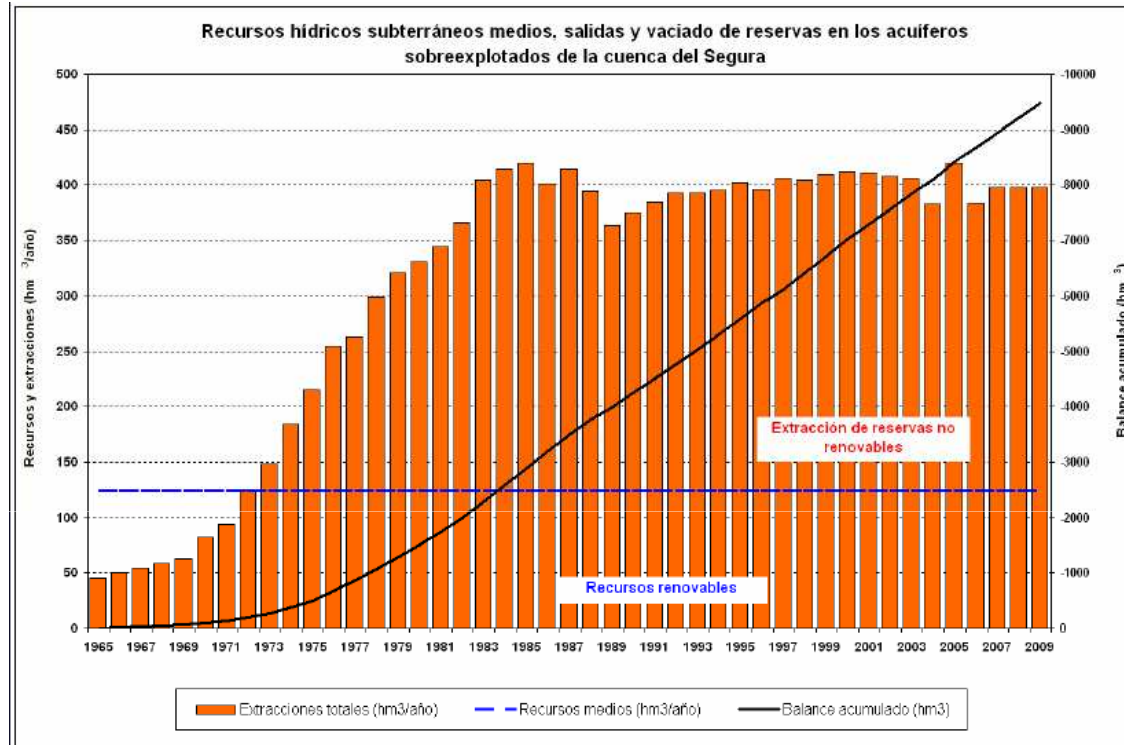


Piezometric level evolution in some of the more intensively exploited aquifers
(Cabezas, 2011, García-Aróstegui, 2013)

Intensive groundwater use and mining in the Segura basin

Total piezometric drawdown
(PHS, 2013)





Cabezas, 2011; Senent et al. 2013

Segura River Basin

Available water resources, hm³/a

Surface water	500
Imported water	400
«Azarbes» (river drains)	40
Reuse	80
Groundwater	
• renewable	240
• non-renewable	170
	<hr/>
	1330

South-eastern Spain and the Canary Islands



Main water streams, desalination plants, and aquifers in South-eastern Spain

Groundwater use

(modified from De Stephano et al., 2013)

Área	hm ³ /year				
	Spain	Xúquer	Segura	CMA	Canaries
Urban	1500	320	—	140	125
Irrigation (C)	5000	1180	450	377	210
Industry	300	100	—	3	8
Recreation	65	10	—	20	12
Total groundwater(A)	7000	1610	485	540	355
Total water (B)	31500	3156	1850	1225	510
A/B groundw/total	0,22	0,51	0,26	0,44	0,70
C/A	0,71	0,73	0,93	0,70	0,59
irrig/groundwater					

South–eastern Spain and the Canary Islands

Use and economic value of groundwater for agriculture
(modified from De Stephano et al., 2013)

Área		Spain	Xúquer	Segura	CMA	Canaries
Total irrigated surface,	10 ³ ha	3345	490	200	210	25
Groundwater irrigated surface,	10 ³ ha	945	160	70	85	25
Total use, hm³/a		12000	1655	800	755	170
GW use	hm ³ /a	3220	535	270	310	170
Production, M€/yr, for total		15300	2260	1450	2460	340
Production, M€/yr, for GW		4730	410	585	1385	340
GW / total use		0,31	0,18	0,40	0,56	1,0
Prod. / surface for total	€/ha	4600	4600	7200	11700	13600
Prod. / surface for GW	€/ha	5000	2600	8400	16300	13600
Prod. / use for total	€/m ³	1.3	1.4	1.8	3.3	2.0
Prod. / use GW	€/m ³	1.5	0.8	2.2	4.5	2.0
Endowment for total	m ³ /ha/a	3590	3380	4000	3600	6800
Endowment for GW	m ³ /ha/a	3410	3345	3860	3650	6800

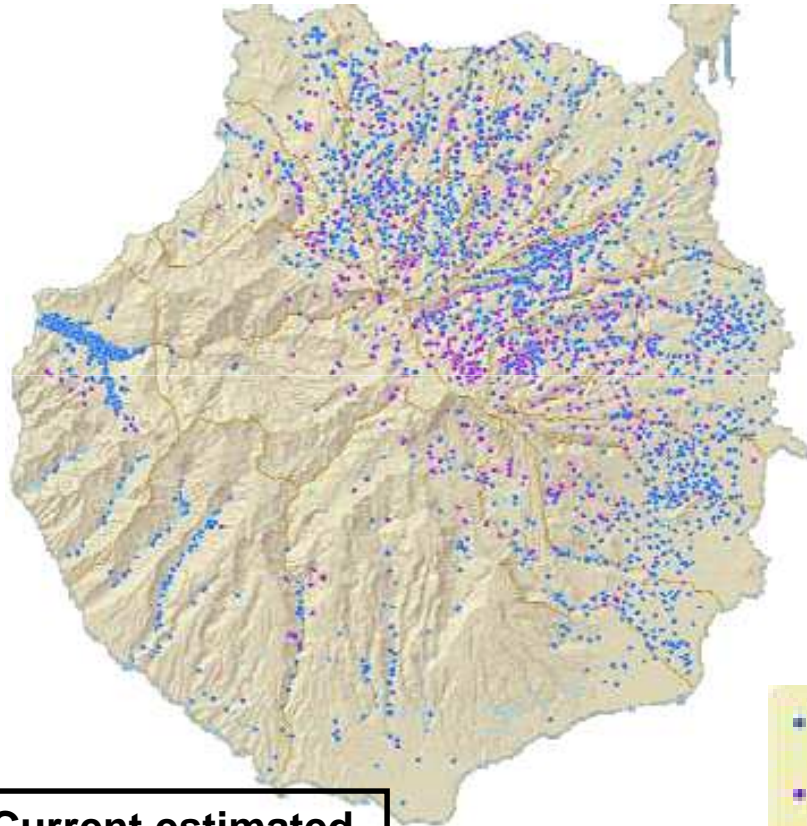
**Preliminary estimation of groundwater reserve consumption.
 South-eastern Spain.
 Period 1980–1995**

Área	Groundwater reserves, hm ³			Consumption rate hm ³ /a	Time to depletion, years
	Consumed, 1980–1995	Existing	Usable		
Almería	800	1100	750	50	15 (10–75)
Murcia	2000	10000	7100	125	60 (10–80)
Alacant	1000	7000	6000	50	120 (10–400)
Valencia	100	2500	200	15	130 (20–350)

(DOGH–ITGE, 1997)

Current estimated total groundwater mining: 15 km³

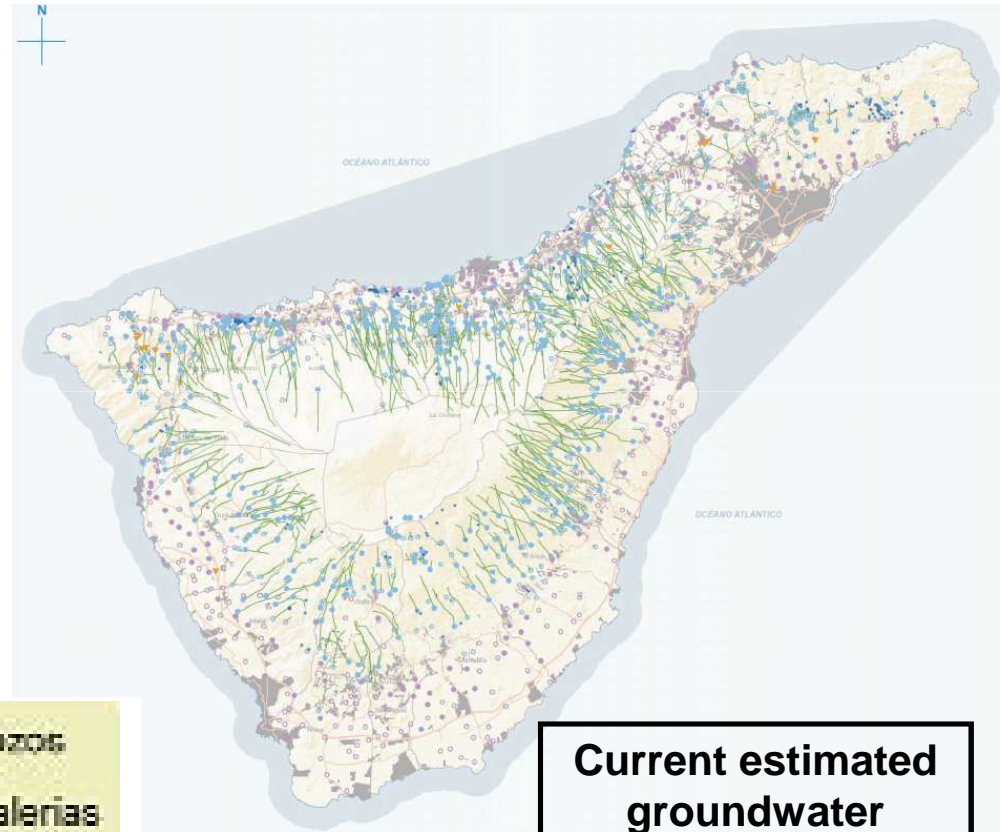
Groundwater in Gran Canaria and Tenerife: Canary Islands



Current estimated groundwater mining 0.3–0.5 km³

Gran Canaria

- Pozos
- Galerías
- Sondeos

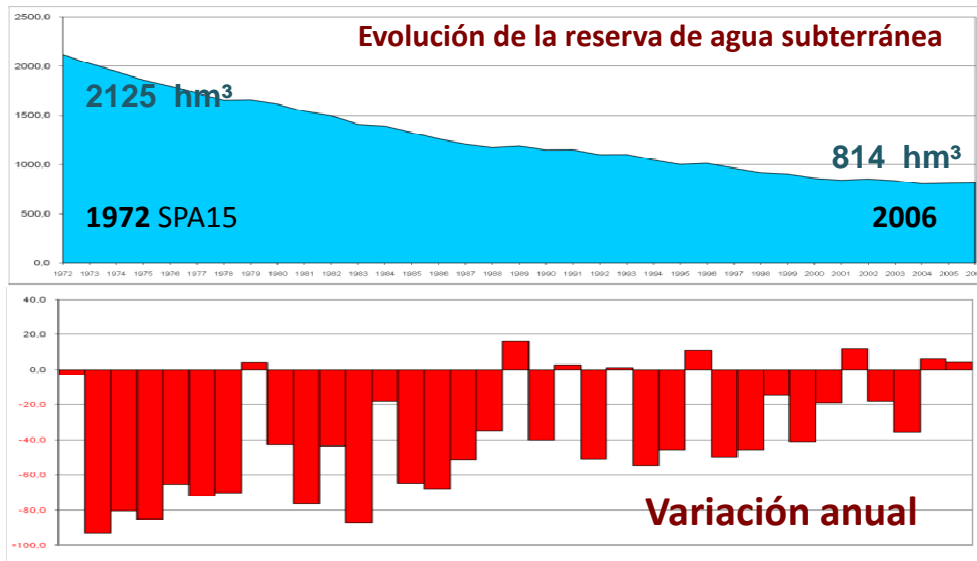


Current estimated groundwater mining 2 km³

Tenerife

Wells and well-shafts; Water galleries (water tunnels); Boreholes

Groundwater reserve evolution in Gran Canaria Island aquifer



Evolution of groundwater reserves

Annual changes of groundwater reserves

Water table depth in a high- altitude, deep borehole →

Groundwater abstraction reduction due to the high cost pumping



Groundwater evolution of Tenerife

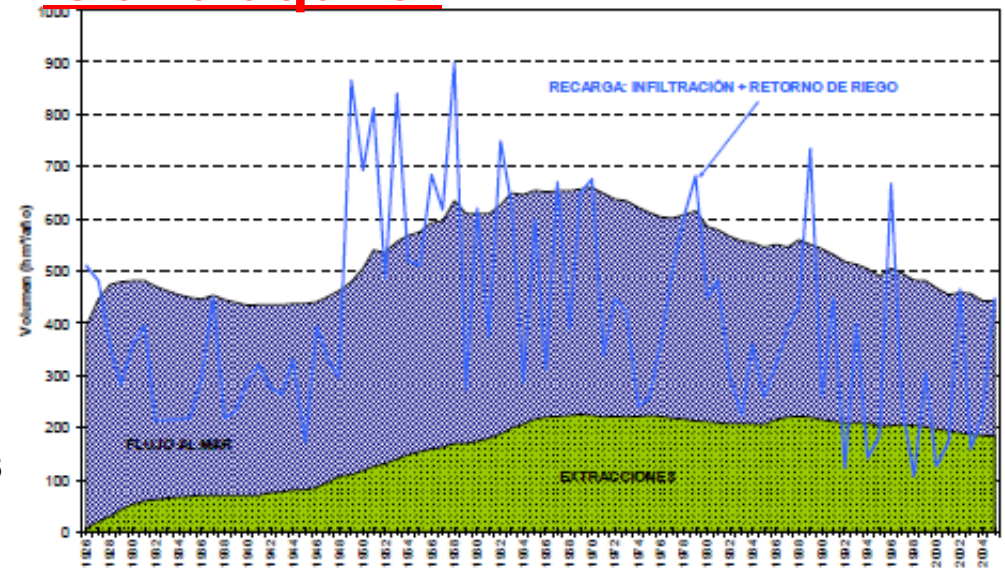
Island aquifer

(PHTF, 2010)

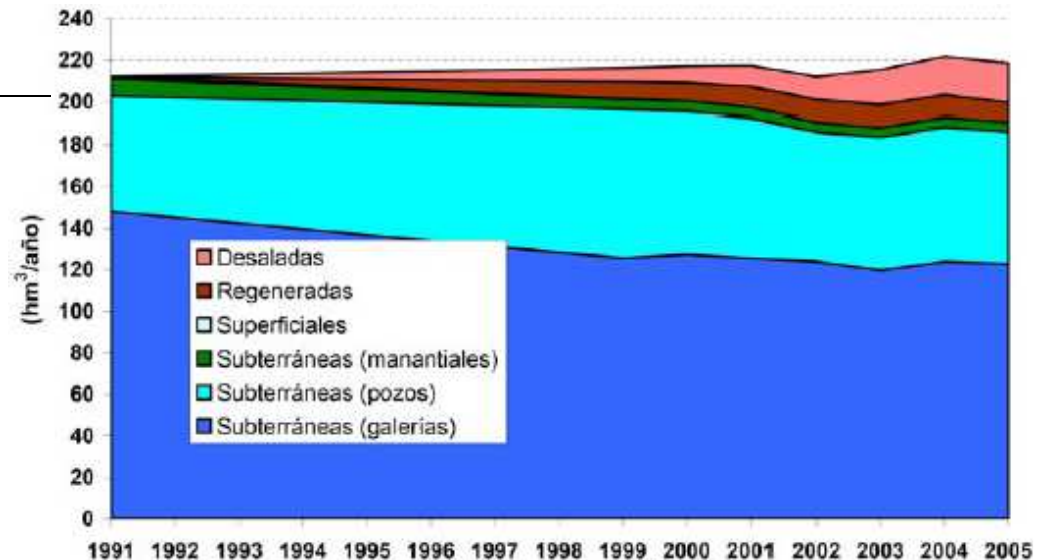
Evolution of groundwater balance components (ETITF, 2008)

Decade	1971–1980	1981–1990	1991–2000	2001–2005
Input, hm³/a				
Recharge	338	321	235	279
Irrig. return flows	93	55	38	27
TOTAL	431	376	273	306
Output, hm³/a				
Abstraction	218	213	205	188
To the sea	399	342	294	266
TOTAL	617	555	498	456
Reserve decrease	186	179	225	148

Large water table drawdown
Important groundwater outflow to the ocean
Large rock volume drained
by mid- and high-altitude water galleries
→ non-recoverable



Groundwater balances



Desalination; Wastewater reclamation; Surface water; Springs; Wells; Water galleries

Groundwater quality issues

Salinity problems {

- Climatic effects in the southern areas of the Canary Islands
- Coastal effects (seawater contamination) along the Mediterranean coast
- Return irrigation flows in many areas (poor irrigation water)

Other natural groundwater quality problems:

- gypsum and halite dissolution from sediments in the Mediterranean area and the Ebre River basin
- high Na–HCO₃ in Tenerife and Gran Canaria Islands
- high F in Tenerife Island

Anthropogenic groundwater quality problems: high NO₃, up to several 100s mg/L

De-brackishing of groundwater and others:
 practiced in Barcelona, Campo de Cartagena and Gran Canaria

Groundwater quality in droughts: **In some cases deterioration due to deep groundwater mobilisation**

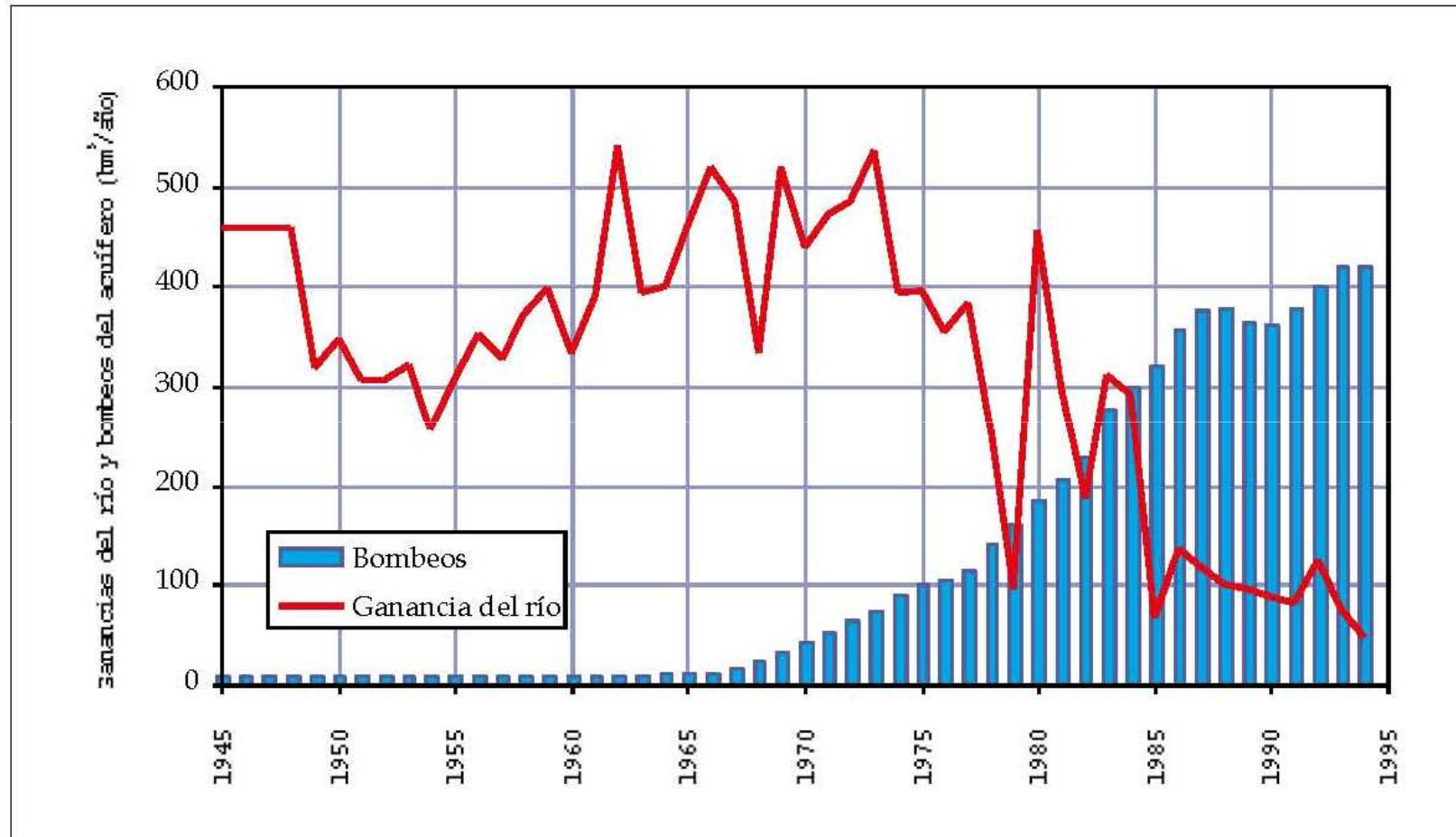
Until present poor attention → water quantity issues dominate
 → water mixing is common
 except for some large water supply systems: Barcelona
 Treatment for groundwater quality is costly → more attention is paid

- debrackishing
- nitrate reduction

 Prospect for improvement {

- when the aquifer functioning is known
- by improving the current poor well construction technology

Environmental effects: on rivers

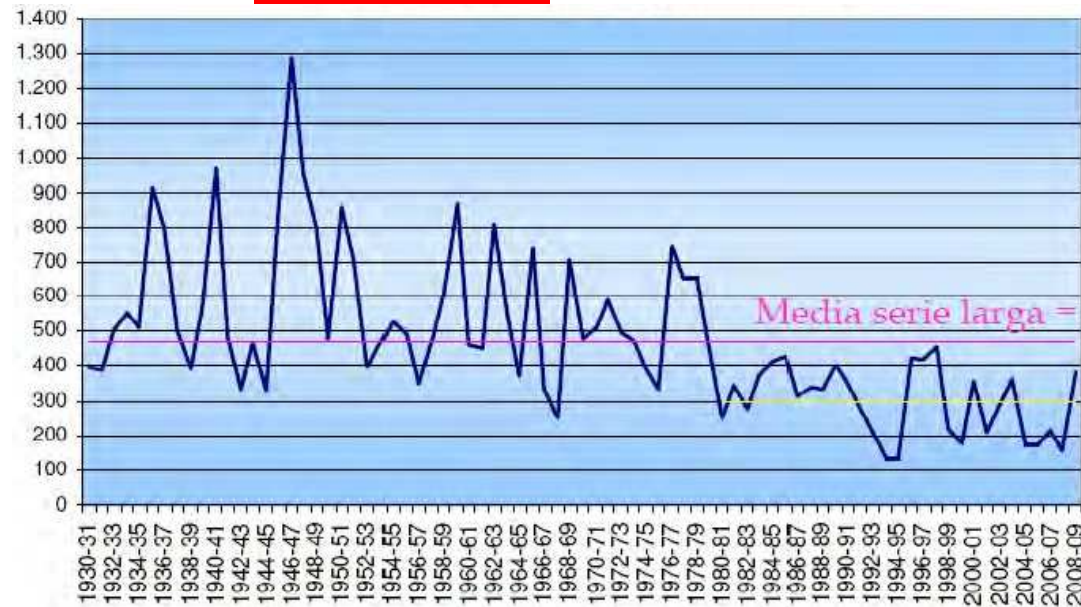


Júcar River flow decrease due to development of the La Mancha Oriental aquifer for agricultural irrigation at the upstream part of the basin.

MIMAM, 2000

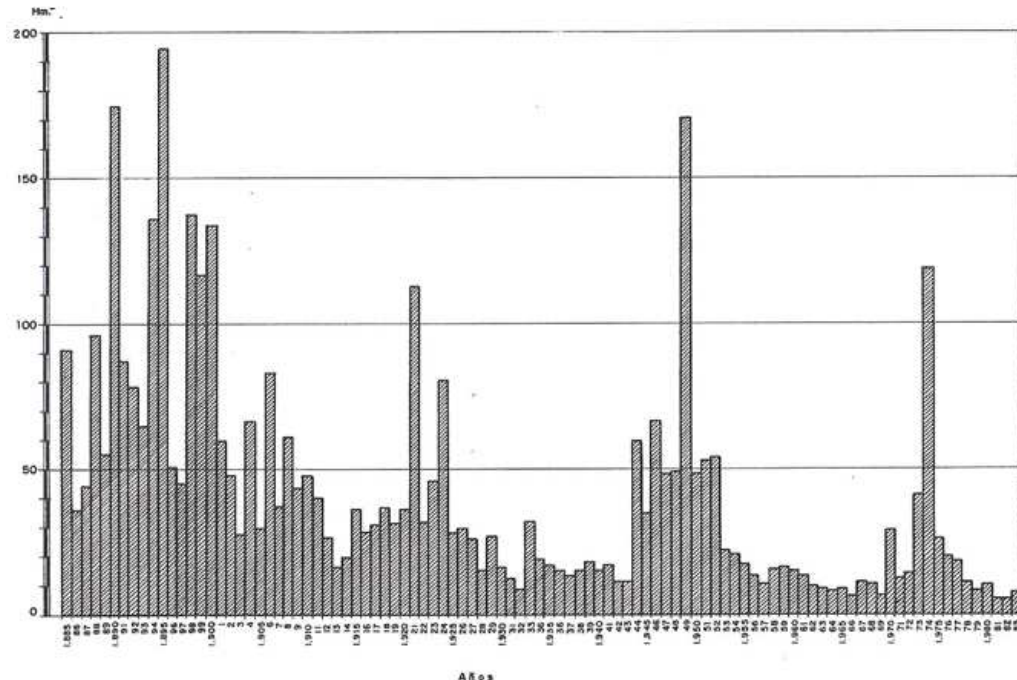
Environmental issues related with intensive groundwater use development

Segura River flow decrease
 Partly explained by increasing upstream groundwater development
 Most of depletion is due to surface water use



Upper Guadalentín River flow decrease
 Not explained by upstream groundwater development

Causes of river flow decrease are not always well explained



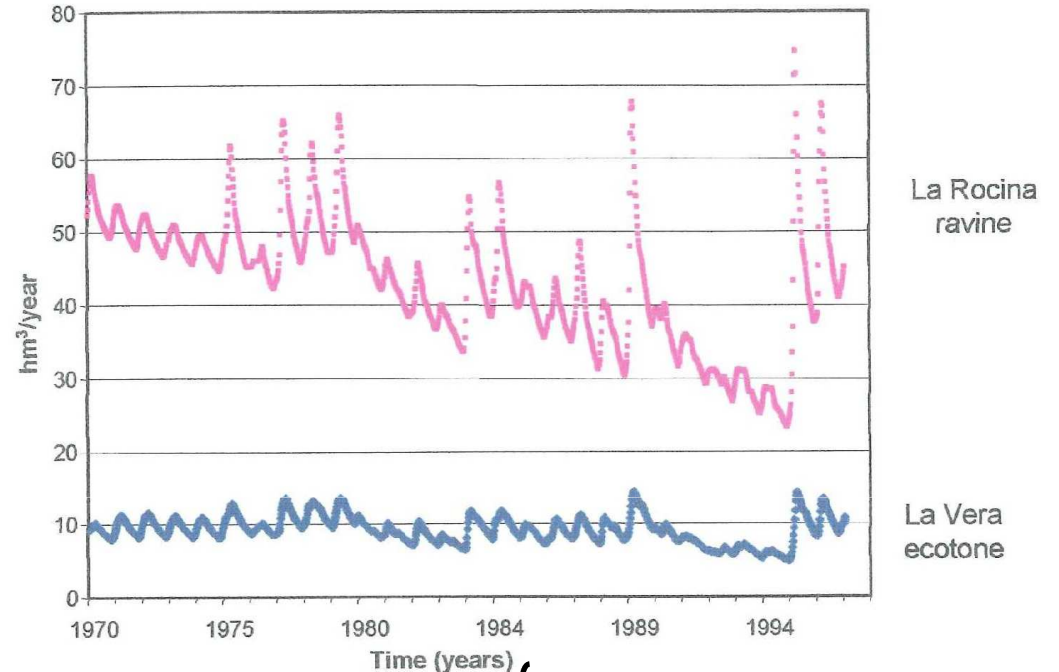
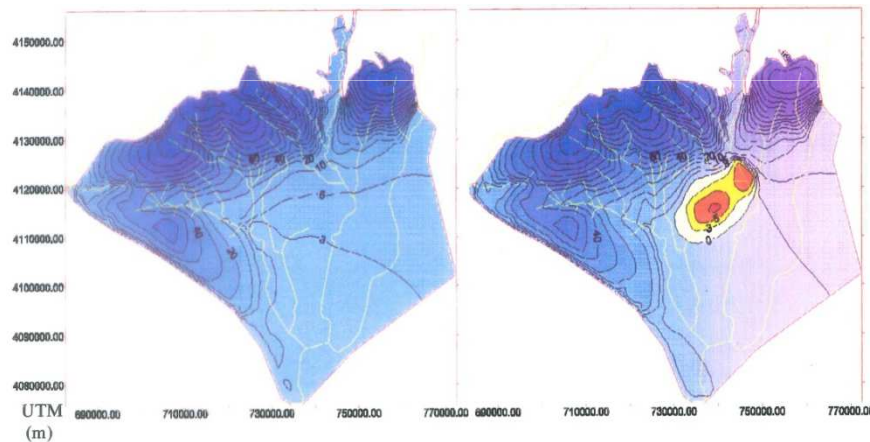
Environmental effects: Doñana National Park

The largest natural park in Western Europe
 A Ramsar site and UNESCO protected area

Groundwater level above mean sea level (m)

Natural conditions
 October 1992

Disturbed conditions
 October 1996



Groundwater discharge to { La Rocina ravine
 La Vera ecotone

Dramatic situation of 1994 → combined effect of:

- cumulated water level lowering due to pumping,
- a 4 years-long drought

modified from UPC, 1999

Large irrigated area with local groundwater.
 Developed mainly in the 1980s

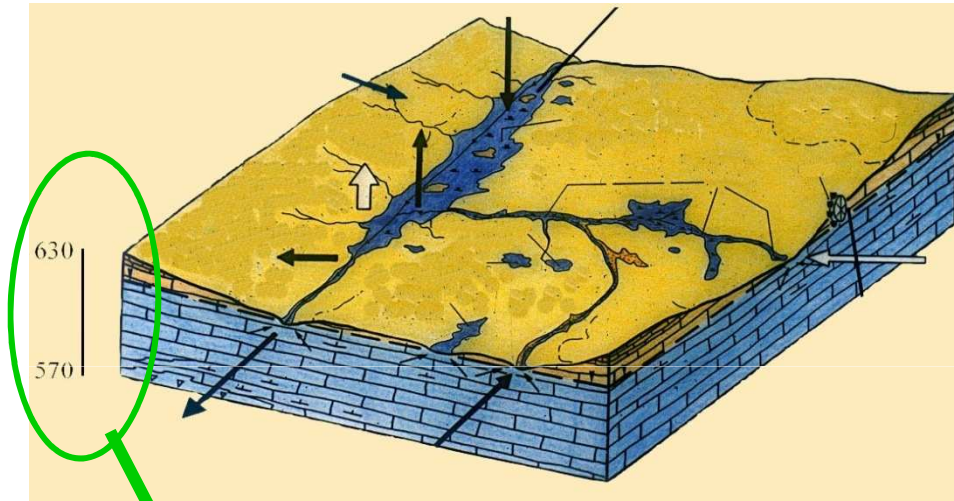
Conflict between { social development
 nature preservation
 Complex governance

Results: northern ecotone dried up
 western and southern ecotone reduced
 decreased / more irregular stream flow
 impairment of lagoons

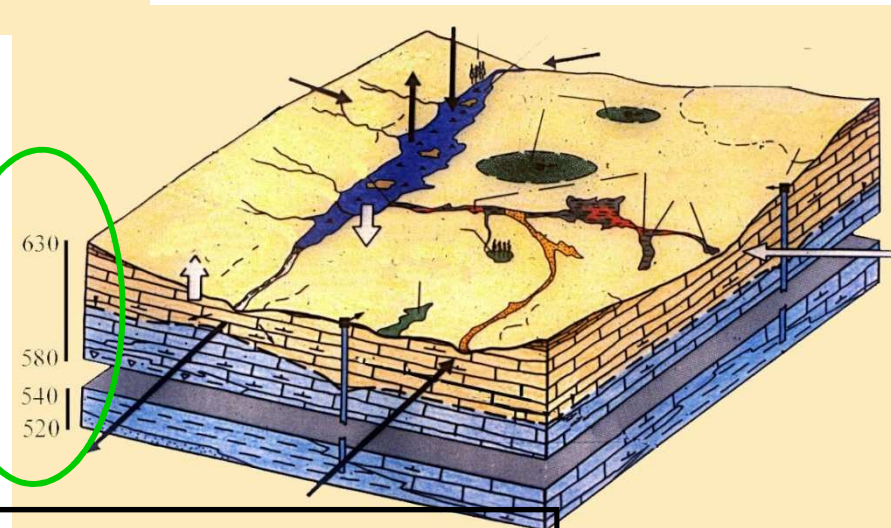
Environmental impacts: Las Tablas de Daimiel wetlands

A key permanent wetland area in Western Europe
 Ramsar site
 UNESCO protected area

NATURAL STATE



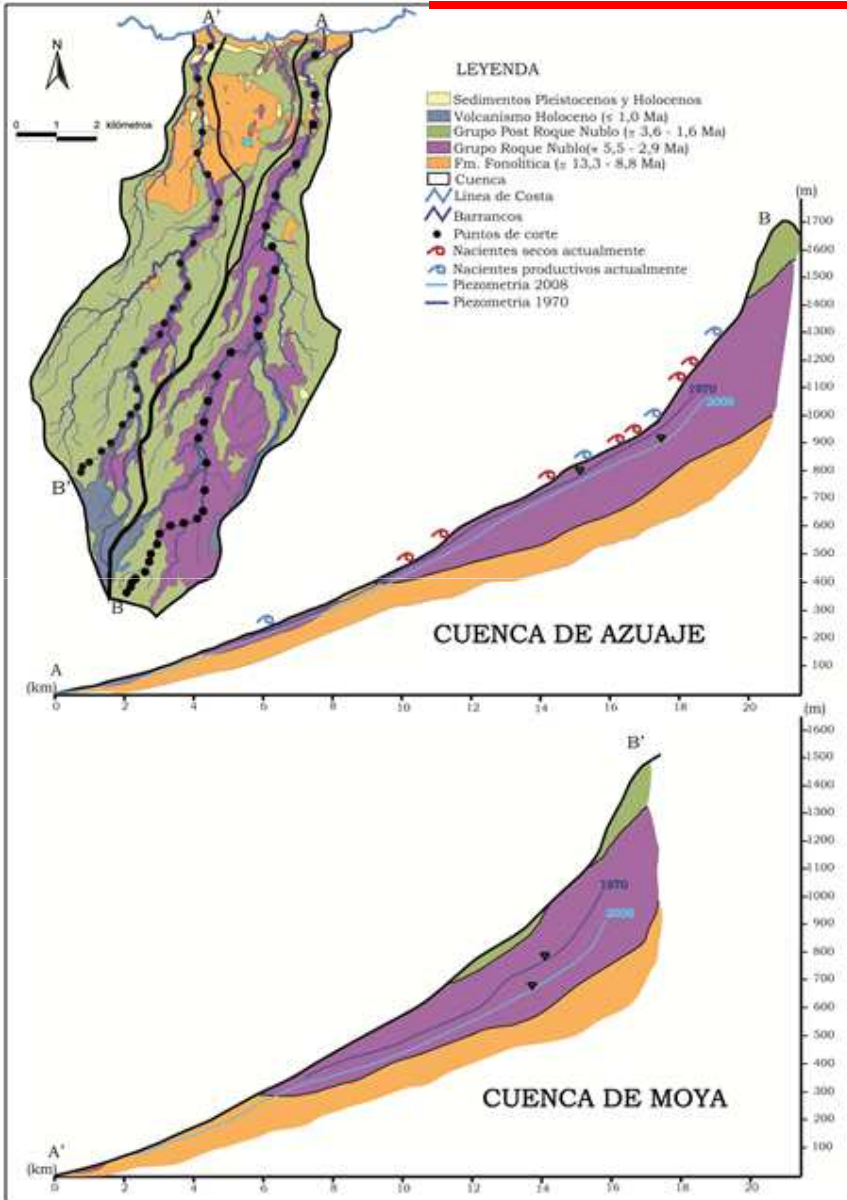
DISTURBED STATE



Significant decrease in piezometric levels; more than 30 m

25 years of conflict between farmers and water authorities / environmentalists
 A partial solution has been agreed

Effects of intensive groundwater exploitation in northern Gran Canaria Island

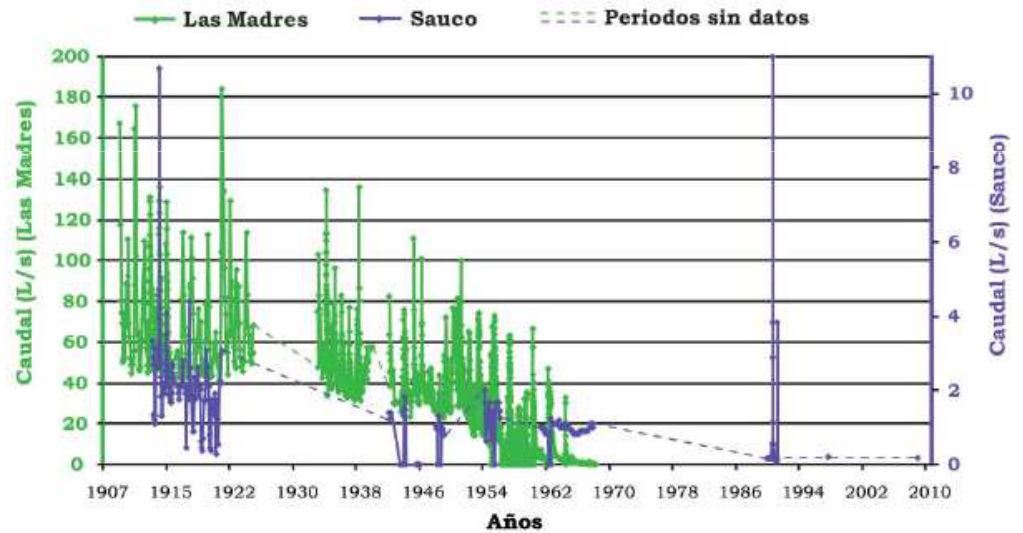


Evolution between 1970 y 2008

Large effects in { spring flow environment other GW developers

Barrancos (gullies) de Moya and Azuaje
 Water-table drawdown. Reserve depletion

Hernández-Quesada et al., 2011
 Cabrera et al., 2014



Springflow decrease, Bco. Azuaje

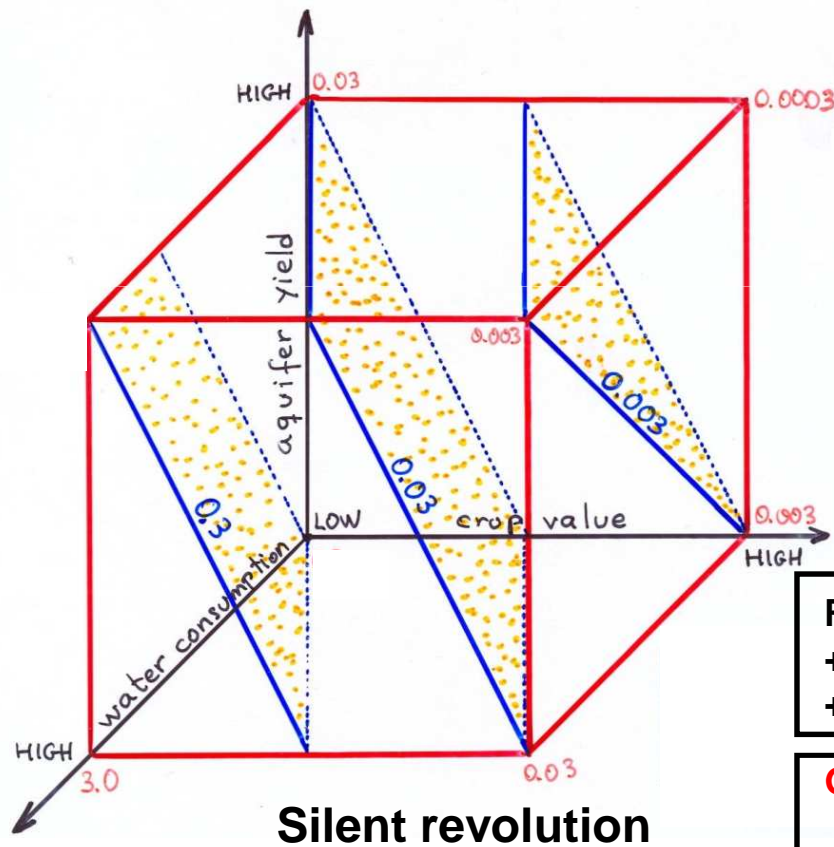
Permanent surface water has almost disappeared
 Few people keep memory of old conditions
 Some present recovery due to high pumping cost

Economic issues related to groundwater intensive use

Groundwater costs and prices

Groundwater as a security investment to cope with drought

Groundwater versus other water sources



(Custodio, 2004)

2015 Botín/Rosenberg-31

Idealized representation of

- agricultural production
- water consumption
- crop value

Shaded plans: surfaces of equal ratio

$$\frac{\text{water cost}}{\text{crop value}}$$

Relatively cheap groundwater + high priced crops + high yielding aquifers	}	→ { <ul style="list-style-type: none"> • almost non-stopable <li style="text-align: center;">GW development • silent revolution
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Groundwater abstraction costs in stressed areas

- high → 0,4 to 0,5 €/m³ → up to 1,0 €/m³
- still cheaper than water from other sources in the site
- subsidies distort the concurrence
- important role in droughts

Socio-economical issues related to groundwater intensive use

Taxation → early attempts failed

even to get resources for monitoring / administration

Trading of public water rights → just starting in the South-east
 short experience
 some reluctancy of water right holders
 close control by water authorities

Trading of private water rights

- common in some areas of Peninsular Spain, especially in the South-east
 - bilateral agreements
 - poorly known
 - limited importance
- well established in Gran Canaria and Tenerife, and to some extent in La Palma Islands
 - old tradition in **water markets**
 - trade of { galleries and wells shares for construction
groundwater
+ transportation
 - water produced by public entities is sold in the markets
 - partly subsidized → control of prices
→ less incentive for private investment

Increase of water offer by public entities is partly **subsidized**

- to respond to social and political pressure
- to try to { reduce groundwater mining
increase environmental water flows

Groundwater institutions

Large and old experience in water users' institutions to manage their water

- mostly for surface water
- rarely involved in resource management and protection

Scarce **institutions** for groundwater resources management

- 10 groundwater user's association already exist
- the first one started in 1975, when groundwater was in the private domain
- it is the most effective → town suppliers and industrialists
difficult to form when farmers dominate
- existing ones have been highly effective in {
 - monitoring
 - control
 - agreeing with authorities
- created bottom-up
- poor results if top-down to comply with legal requirements in areas declared "overexploited"
- key institutions to cope / tame drought effects

Poorly structured **civil society**

- partly displaced by political action
- lack of experience in using their {
 - vision
 - capabilities

Variable degree of transparency in public water institutions

unclear action during droughts

→ large and costly failures due to lack of transparency (case of Barcelona)

Some considerations related to groundwater mining

- Groundwater **mining** is a fact and **will continue** unless subsidized water is not provided
- The **main deterrent** to groundwater mining are not regulations but
 - { the increasing weight of energy cost
 - { in some cases groundwater quality deterioration
- **Environmental effects** { are poorly known and valued
 { mostly happened decades ago
- recovery { is difficult
 { it may be at a disproportionated cost
 { it may produce damage in some areas
- **Ethical aspects**
 - some slow recovery is possible
 - need of a **change of paradigm** → a difficult task
 - need of groundwater **users involvement** in { monitoring
 { surveyance
 { decision making
 - civil society** should { recover from current poor activity
 { be more concerned
 - politicians should **not overcontrol** groundwater affairs

Prospective

Enactment of a more flexible **Water Act**

→ solve the stiffness of water rights and concessions

Agreement on a **water pact** { among all interested actors
especially among political parties

→ the seed is on the mind

→ this is large ignored by present government

→ its interest centers on water planning (WFD required)

Consideration that **groundwater mining** { is not necessarily evil
in some cases it is good

control it

keep benefits to compensate for current and future damage

consider it as a transient situation with a dead end

Improvement of groundwater mining experience

→ study the experience in other parts of the World

→ develop the **GWM project** to compile worldwide existing experience

Incorporation of **groundwater reserves** into drought management



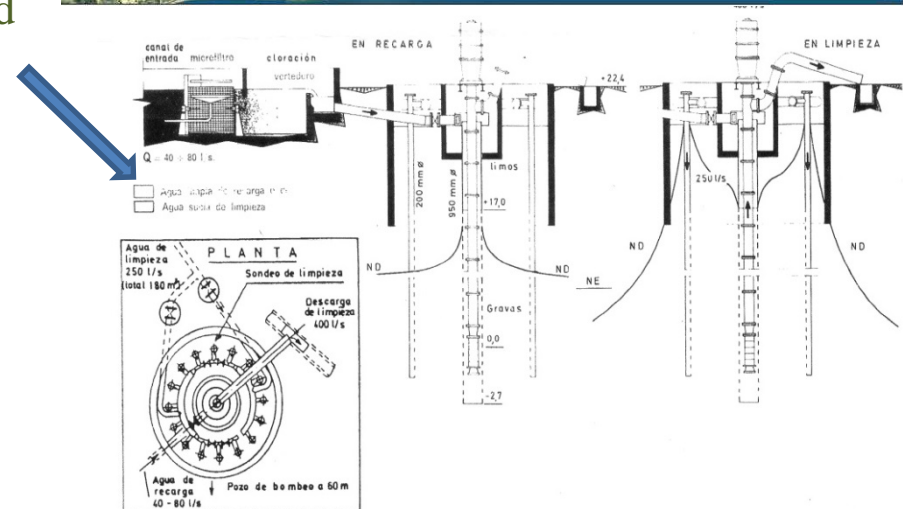
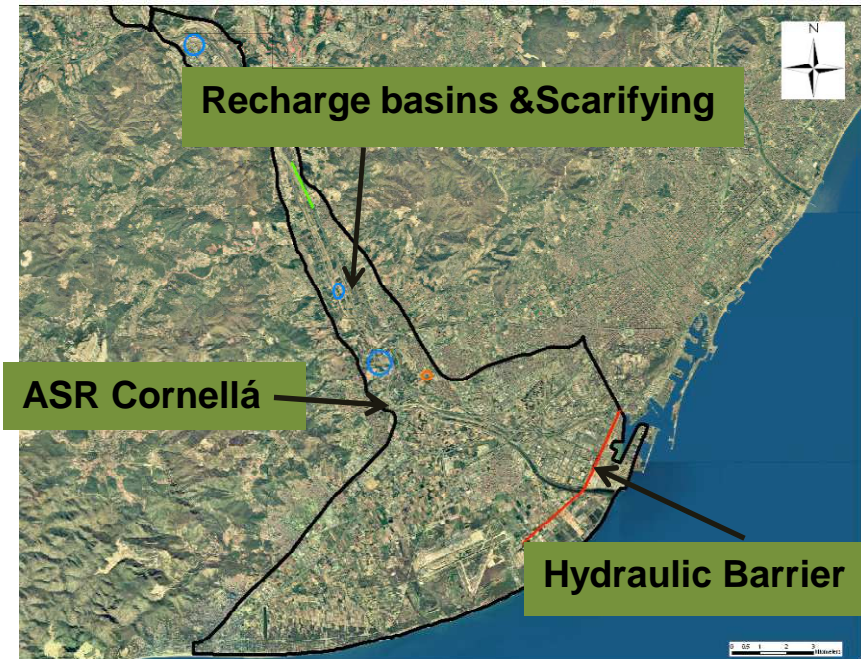
CONJUNCTIVE USE IN SPAIN

• Artificial Recharge

- Supply of the Metropolitan Area of Barcelona
 - Llobregat river
 - » Sea water intrusion Barrier
 - » 12 dual recharge–pumping wells ASR
 - » Recharge basins
 - » River bed scarification
 - Besós river
 - » 2 ASR wells (1954 and 1955).
 - » Pumping and injection well \varnothing 1m and 16 \varnothing 0.2 m to help cleaning

• Others

- Belcaire river (Castellon)
- Algar dam. Purposely leaking dam in limestone
- Canal de Isabel II (Madrid)





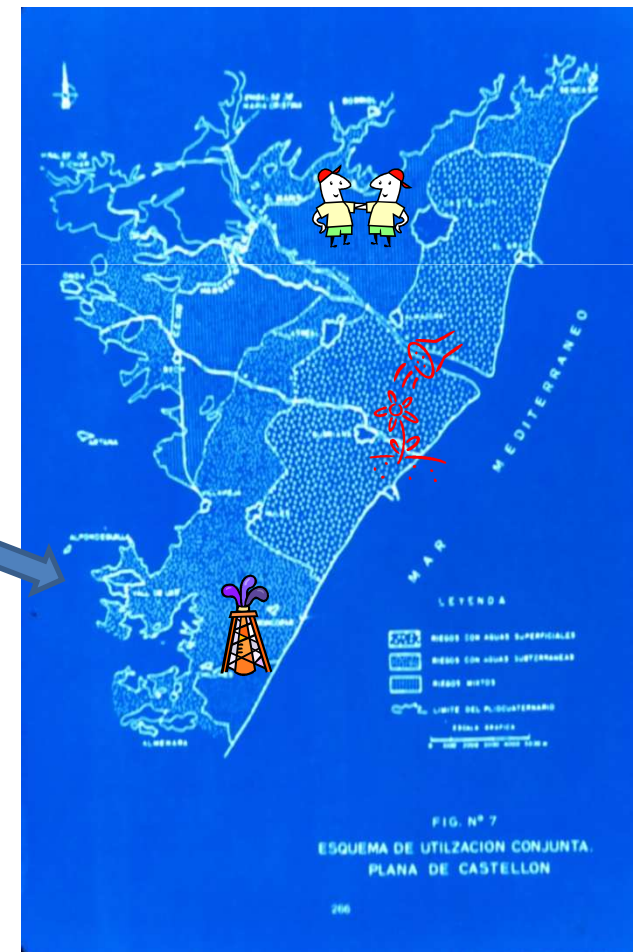
ALTERNATE CONJUNCTIVE USE

Mijares river Plana de Castellón

- Water needs part with surface water
- Part with groundwater
- Remaining parts alternate ways; more g.w in dry years and more s.w in wet

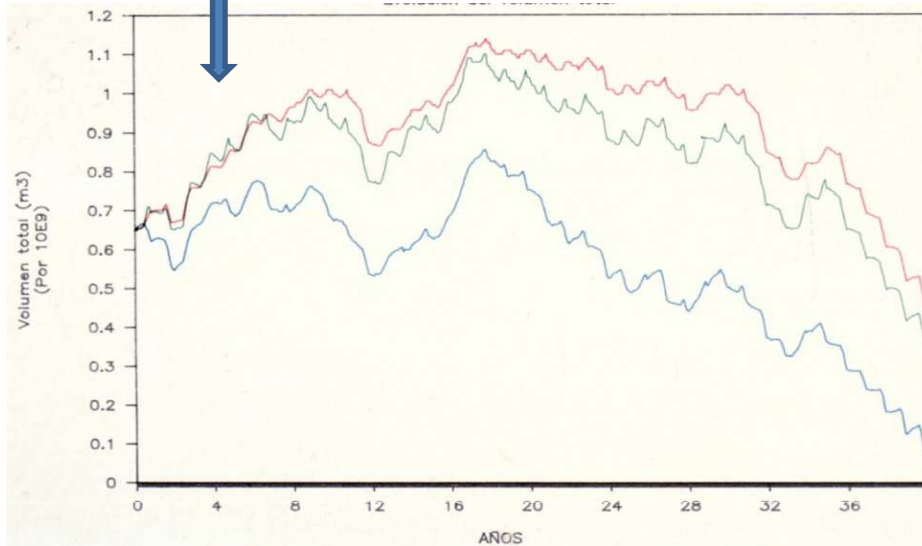
COMPONENTS

- 1 big upstream dam 100 hm³ of storage
- 2 leaking dams in limestone, Sihar Dam 60 hm³ and M^a Cristina Dam 28 hm³
- River losses in Mijares and Rambla de la Viuda
- Irrigation return flows
- Sea water encroachment in the South
- Strategy suggested by users accepted by the Basin Authority in 1973.
- Replaces groundwater extraction with surface water releases
 - Strategy proposed in the CWP 1957, (in-lieu recharge)





Use of storage in the LP de Castellón aquifer



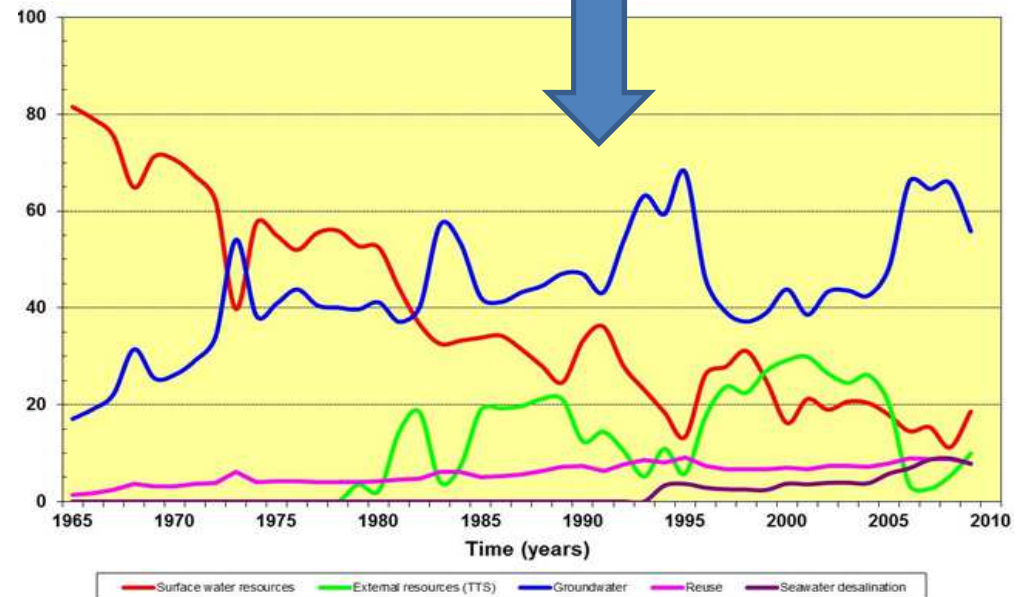
- Aquifer storage used was about 700 hm³ (4 times the storage of dams)
- Increment in the last 2 decades
 - drip irrigation has augmented
 - irrigation with reused treated water.
- Alternate use strategy in several areas of the Júcar Basin
 - In the Palancia Basin started alternate conjunctive use at the first quarter of the last century

- In most aquifers, mainly in droughts, pumping increases

Water supply of Madrid wells, up to 80 hm³/yr. Used mainly in droughts or low storage in dams

2007 drought in the aquifer Plana de Valencia Sur, pumped 50 hm³ from wells given to farmers previously drilled by the Basin Authority

Similarly CH Segura pumped 50 MCM in the alluvial aquifer of the Segura river





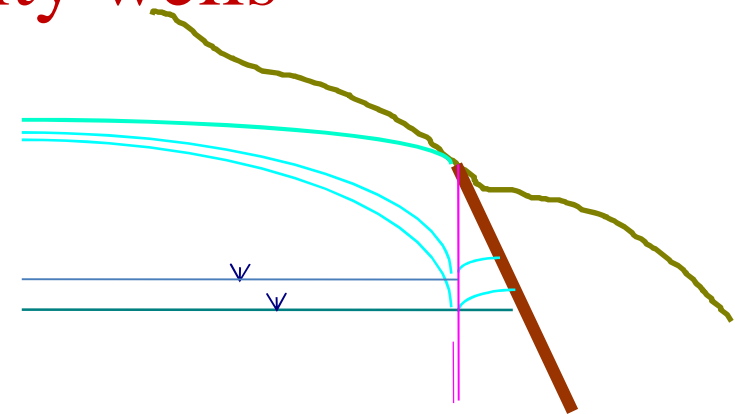
Regulation of karstic springs with nearby high capacity wells

- Abundant carbonate aquifers.
 - Specific yield 1–3%. Low storage capacity, high water level oscillation
 - Quicker impact on surface flows and wetlands
 - Recharge from dams and channel infiltration

Flow of some karstic springs in Spain fluctuates between 0,1–100 m³/s

Topographical conditions often preclude drilling wells away from the spring

- Proximity of canals or conduits allows the transport of pumped water.
- Frequent high flows
 - (850+350)L/s in Los Santos
 - 2,250 L/s in Deifontes (Granada) 5 wells
 - (400+400) L/s in El Algar spring (Benidorm)
 - Arteta spring. Navarra



Conjunctive use in La Marina Baja

2 dams + 2 well fields + 1 pumping station + water reuse (interchange)



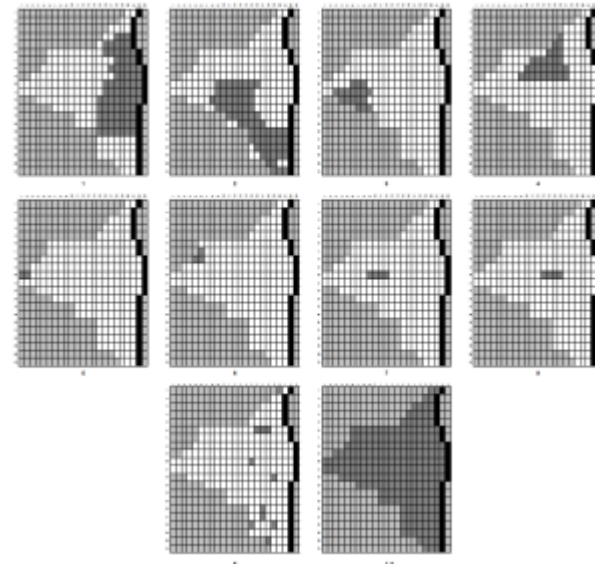


THE EIGENVALUE SOLUTION

An explicit solution that makes conjunctive use modeling easier

- Classical g.w. modeling:
 - in sequential time steps
 - Water heads are obtained in each step by solving a big algebraic linear system of equations.
- But there are other solutions. The continuous in time g.w. flow equation is reduced to a well known Sturm–Liouville problem. It is only valid for N parameters (**eigenvalues**). Each one has its corresponding **eigenvector**.
- The solution is given by a vector \bar{L} of the intensities of each eigenvector.
- \bar{L} is a complete solution in a different basis
 - 0, 0, 0,0, 1, 0 ...0, 0, 0
 - 0, 0, 0,0, 0, 1 ...0, 0, 0, for the Cartesian
 - 0, 0, 0, ... 0, 0,1, 0
- The orthogonal set of eigenvalues for the eigenv
- From the previous \bar{L} situation and the action in the new period a new \bar{L} is obtained easily and explicitly. Instead of heads in the nodes.
- Surface and subsurface components of conjunctive use schemes should be simultaneously simulated.
- When many alternatives must be evaluated, an explicit tool for aquifer simulation would be advantageous.

Modelling process always uses a limited number of unitary elementary actions





Eigenvalues II

- An N&P invariant matrix previously computed multiplied by \bar{L} can provide the following P control parameters
 - Aquifer and river flow interchange in different zones
 - Groundwater heads in different points
 - Groundwater stored in different areas of the aquifer
 - Flows between two zones of the aquifer
- Once computed the eigenproblem and the matrix, it is easy to incorporate to most surface water models and able to simulate jointly and explicitly numerous alternatives
- The complete solution of the eigenproblem is the most demanding task, but it must be done only once
- A very reduced set of \bar{L} 's components is needed to simulate with the same precision as FD or FE
- Oscar Alvarez Villa is his dissertation tested the methodology to a 22.000 cells aquifer that were reduced to a number of linear deposits, 200 to 600
- **Adequate for complex systems, multiple alternatives and climate change uncertainties**

